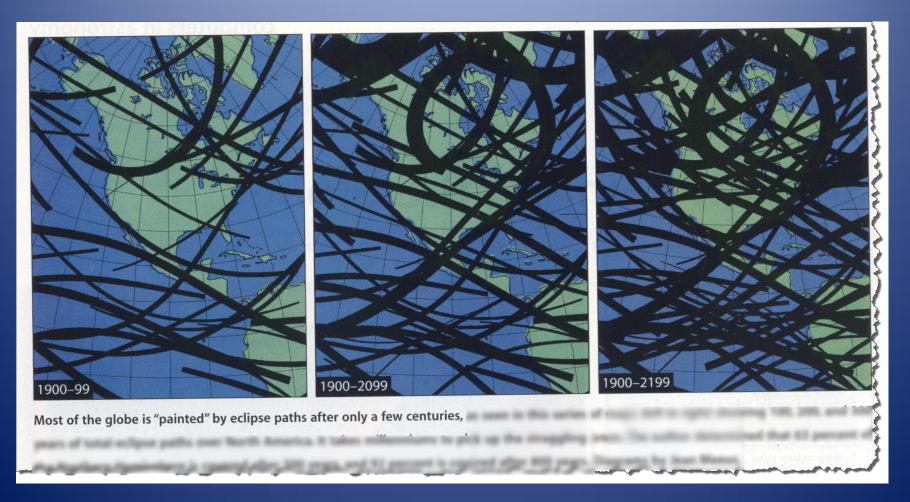
#### More Morsels – SEC2014



john.tilley@cantab.net

#### **Getting hooked on Morsels**

"Shadow Painting the Globe"



### Two Topics

List ALL UK eclipses



### Two Topics

**List ALL UK eclipses** 



- Solar and lunar semester
- The hidden relationship
- Lunation gaps

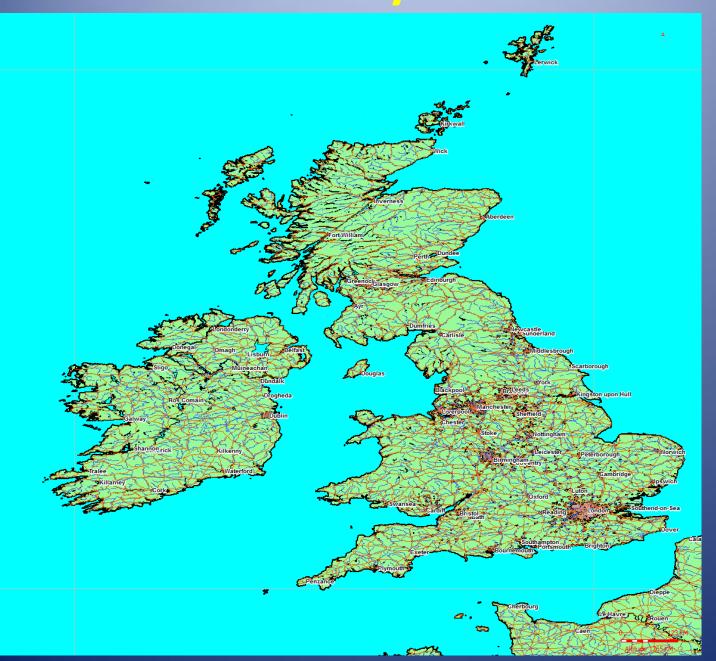
PERIODICITY AND VARIATION
OF
SOLAR (AND LUNAR) ECLIPSES

by

PROF. DR G. VAN DEN BERGH

MCMLV H. D. TJEENK WILLINK & ZOON N.V. - HAARLEM

#### **How many countries?**



Challenge
Produce lists
of ALL

- •Partial
- •Annular
- •Total eclipses For ALL countries
- •From -1999 To +3000

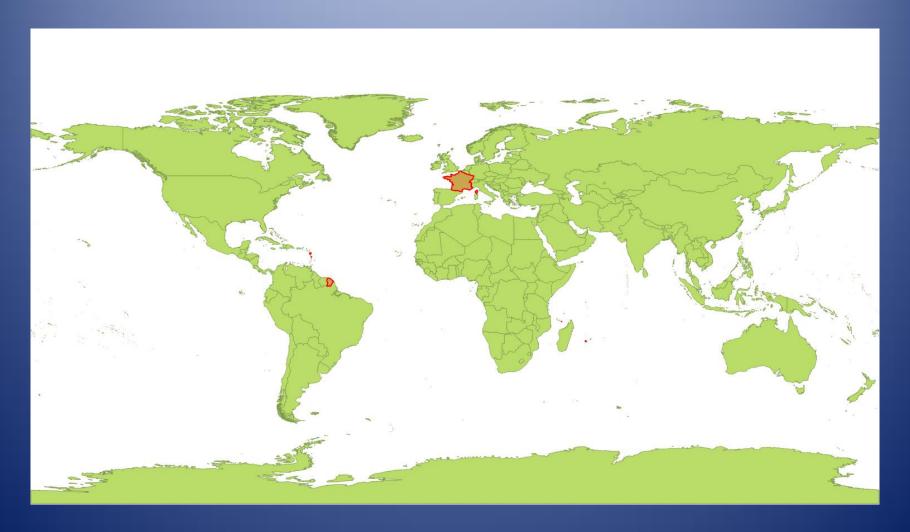
How???

#### Country and mapping data



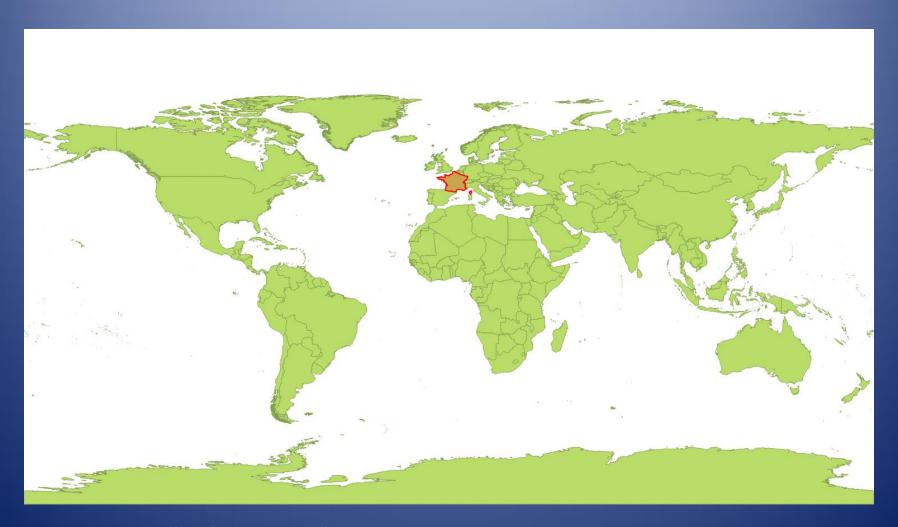
Vector Data	Number		
Sovereign States	197	Greenland part of Denmark	
Countries	254	France includes some territories	
Map Units	291	Australia includes remote island	
Map SubUnits	351	USA = 48 states + Hawaii + Alaska	
States/Provinces	3671	In most cases too much data	

#### 254 Countries



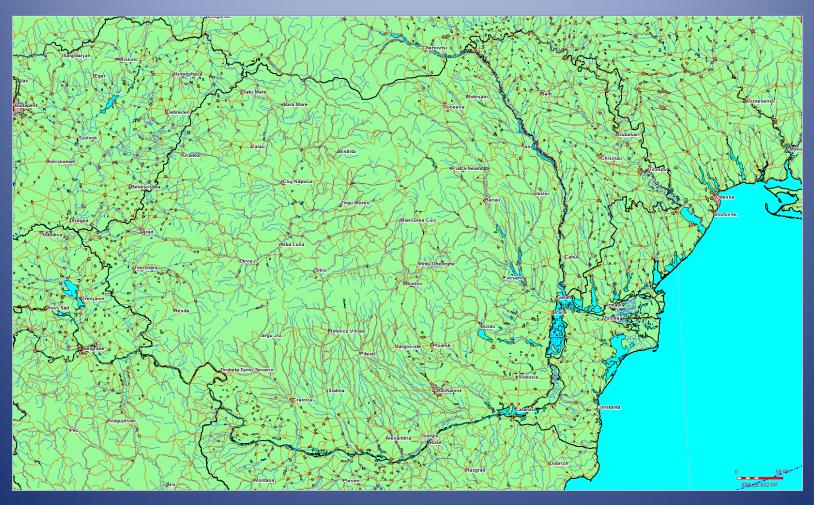
France = Mainland France, Corsica, French Guyana, Caribbean, Indian Ocean.

#### 291 Map Units



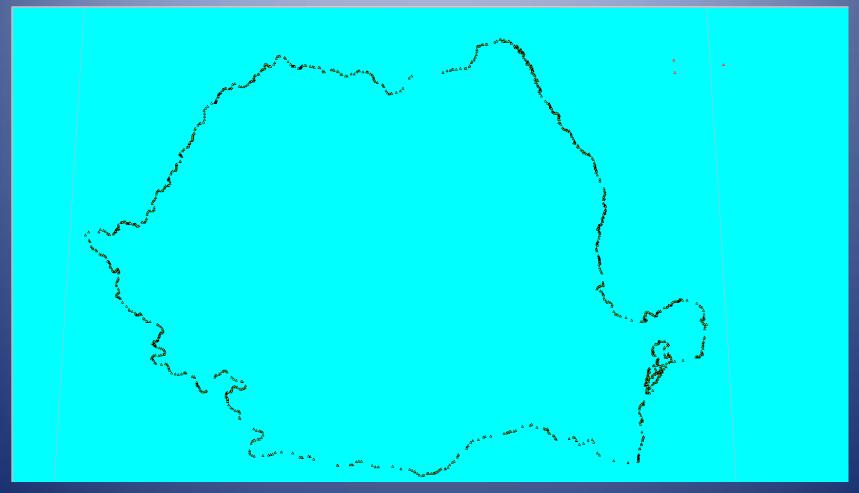
France = Mainland France and Corsica

#### Romania



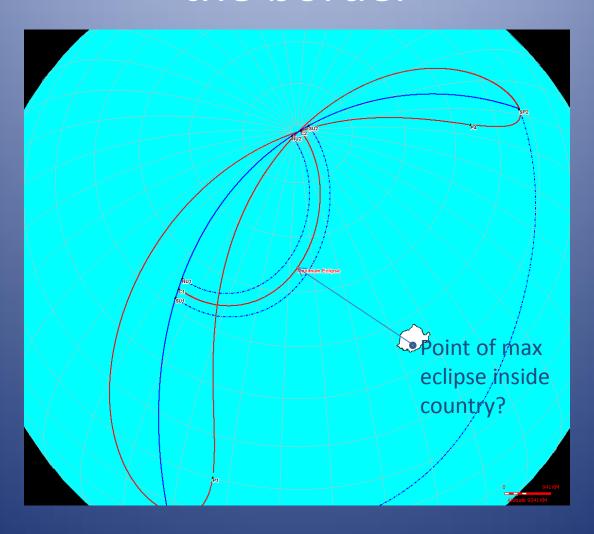
5 layers of data = Country border, lakes, rivers, roads and built-up areas Country border is key

#### Romania border as points



1201 pairs of border points in NEV10m – there are some "large" gaps Can find local circumstances for EACH border point Eclipse Y/N, type, magnitude – hence max eclipse on country border

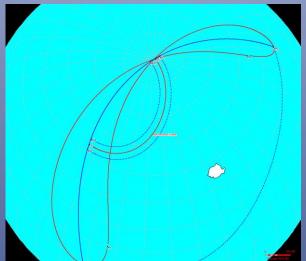
# Country maximum eclipse MUST lie on the border

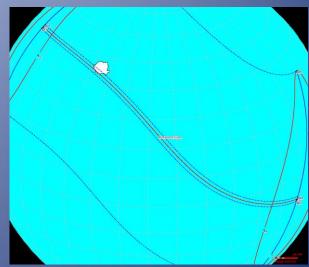


#### Luca's Algorithm

"For any given country and for any given solar eclipse, the point of country maximum eclipse must lie on that country's border, unless the point of maximum for the eclipse as a whole lies inside that country. "







Track of totality crosses
Romania

- -Romania sees a total eclipse
- Point of maximum for the eclipse as a whole (August 1999) actually lies inside
  Romania

Track of totality lies outside Romania

- -Romania sees a partial eclipse
- -Max eclipse visible in Romania must lie on the border

Track of totality crosses
Romania

- Romania sees a total eclipse

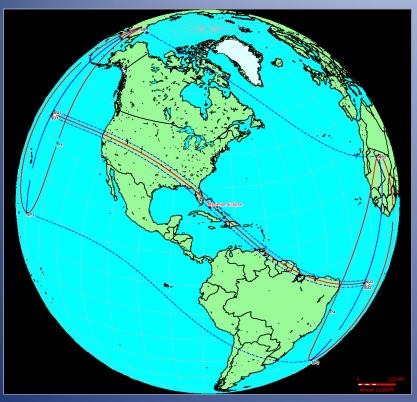
Max eclipse visible in Romania must lie on the border

#### **Eclipses by Country Number Crunching**

- Natural Earth Vector 1:10million
  - 291 "countries"
  - 553176 points
  - 11898 solar eclipses
  - 6.58 billion calculations
  - Note some special cases
    - Not yet fully handled



#### **USA Solar Eclipses**

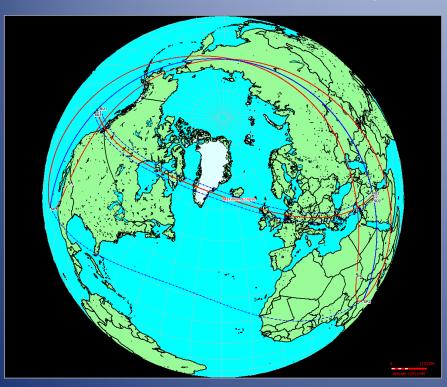


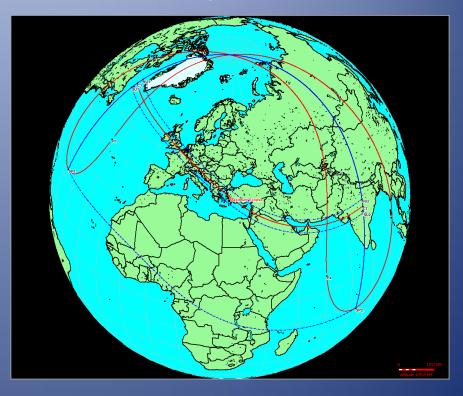
617 total723 annular3810 partial

In 5000 years

- 8 total eclipses exceed 6minutes duration in USA
- 2045 August 12<sup>th</sup> total 6m 6sec
  - 12 lunations after 2044 Aug 23<sup>rd</sup> total eclipse

# Eclipses with most countries to see totality or annularity

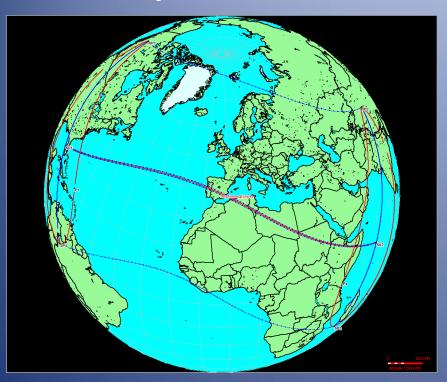


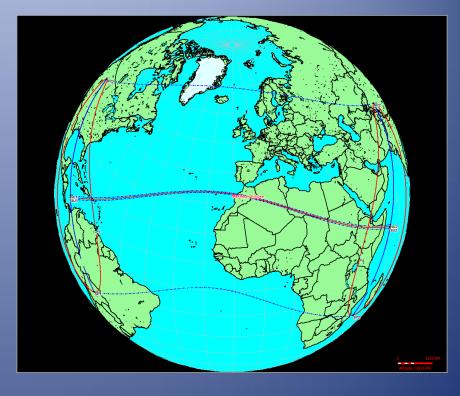


1433 June 17<sup>th</sup>
Total in 39 countries

-1763 October 8<sup>th</sup>
Annular in 53 countries

#### Eclipses visible in most countries





Total eclipse 1600 July 10<sup>th</sup> 212 countries
Total in 11 countries
Partial in 201 countries

Annular eclipse 410 June 18<sup>th</sup> 210 countries
Annular in 11 countries
Partial in 199 countries

## **Total Eclipses by Country**

- 3171 pure total
- 571 hybrid eclipses in5000 years

	А	D
1	Country	#Total
2	Russia	634
3	United States of America	617
4	Brazil	495
5	China	459
6	Canada	447
7	Australia	427
8	Antarctica	392
9	India	355
10	Chile	347
11	Indonesia	321
12	Argentina	302
13	Japan	256
14	Democratic Republic of the Congo	245
15	Mexico	241
16	Kazakhstan	213
17	Algeria	213
18	Colombia	213
19	Sudan	207
20	Peru	196
21	Saudi Arabia	195

## Annular Eclipses by Country

- -3956 pure annular
- 571 hybrid in 5000 years

	А	В	D
1	Country	#Annular 💌	#Total
2	United States of America	723	617
3	Russia	698	634
4	Antarctica	567	392
5	Brazil	546	495
6	Australia	510	427
7	Canada	490	447
8	China	489	459
9	Chile	412	347
10	India	402	355
11	Indonesia	376	321
12	Argentina	370	302
13	Japan	288	256
14	Democratic Republic of the Congo	273	245
15	Mexico	272	241
16	Peru	255	196
17	Kazakhstan	244	213
18	Algeria	242	213
19	French Polynesia	233	157
20	Myanmar	231	190
21	Mozambique	231	167

#### Special Case 1

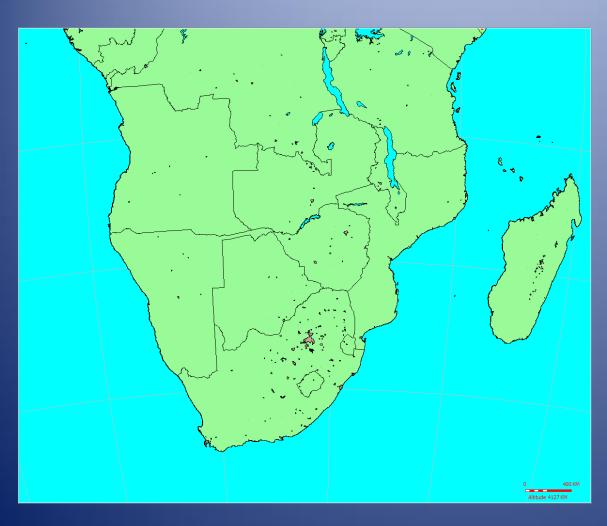
- Eclipse track is very narrow and passes between adjacent points on boundary
  - Eclipse misclassified
  - Hybrid eclipse 164 March 10<sup>th</sup> in Peru
  - Totality 3 seconds
- Use binary search to find point of greatest eclipse on boundary

#### Special Case 2

- 2379 March 19<sup>th</sup>
- Grazes Austrian border
- Amount of detail in digital mapping can change the type or duration

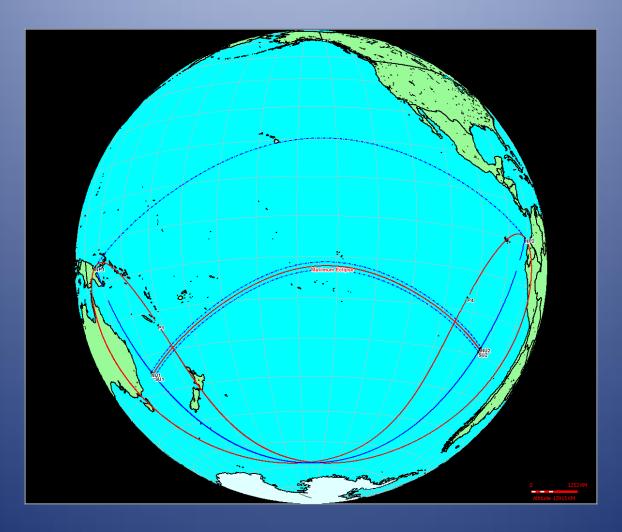


#### Special Case 3



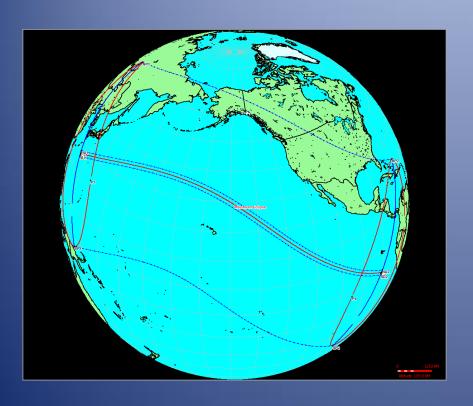
Lesotho is wholly inside South AfricaCheck "Point in country" algorithm implementation returns correct country name!

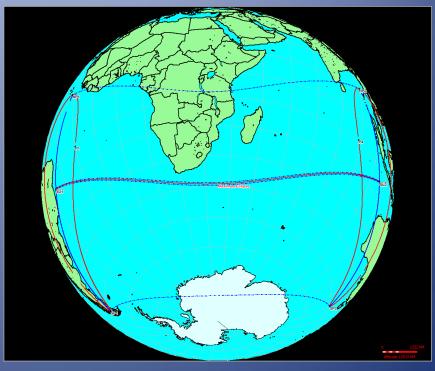
#### Aqueous Eclipses (MAM5)



Total eclipse 2310 May 29<sup>th</sup> (5m 10sec) misses all Pacific islands

#### Aqueous total eclipses



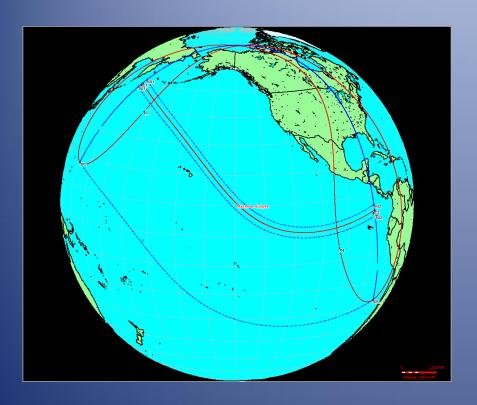


Longest 6m 6s in 222 July

Next eclipse 2m 28s in 2057 Jan 5th

74 total aqueous eclipses in 5000 years

#### Aqueous annular eclipses



LEZZO ZOLAZ ZOLAZ

Longest 10m 44s in -249 November

Next eclipse 22s in 2032 May 9th

97 annular aqueous eclipses in 5000 years

#### **Lunation Gaps**

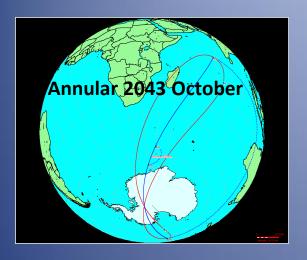
- Gaps between USA total eclipses
- Longest gap is 587 lunations
- Shortest gap is 6 lunations
- Gap to 2017 from 1991 is 323 lunations



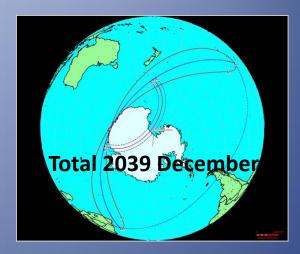
#### Quiz Question 1

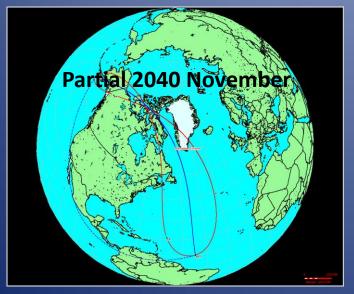
 Can you see totality in Antarctica on the Summer Solstice – i.e. June?

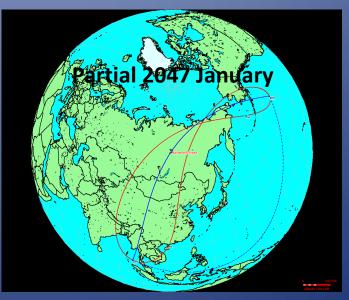
#### 5 interesting eclipses in next 35 years



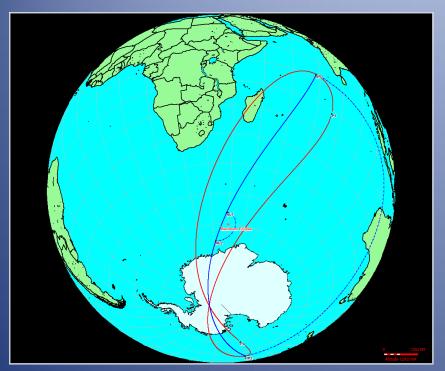


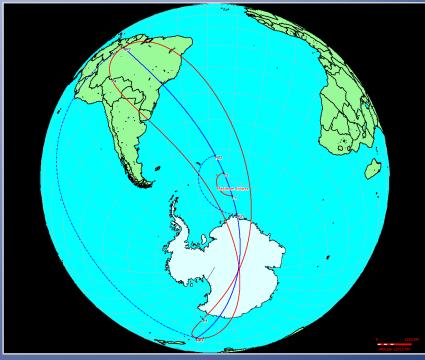






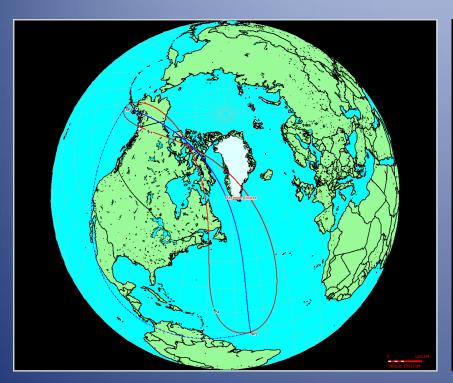
#### 2 Annular eclipses 5 Iunations apart

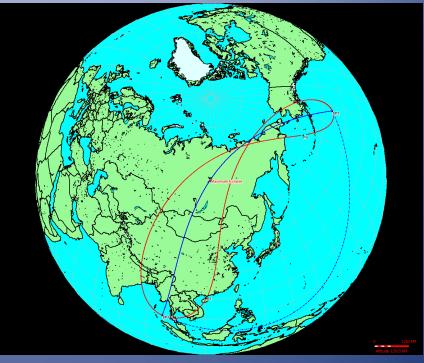




Smallest possible gap between annulars 4 such pairs in 5 millenia Canon Pair in -1461 overlap on land

#### 2 Partial eclipses 77 lunations apart





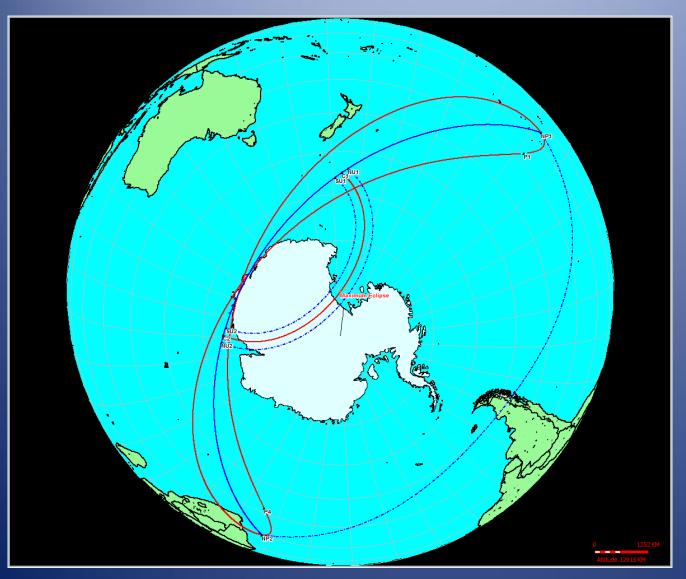
77 lunations is longest gap in 5 millenia Canon and longest gap in 26000 year Canon 12 consecutive total or annular eclipses

Mentioned in Meeus "Elements of Solar Eclipses"

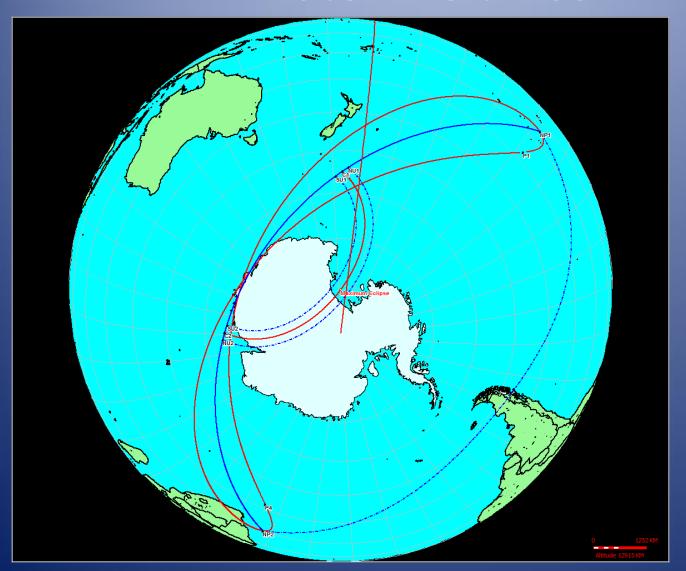
#### Shortest gaps between eclipses

	Eclipse Type	Lunations
Solar	Partial	1
	Pure Annular	5
	Pure Total	11
	Annular and hybrid	5
	Total and hybrid	6
	Hybrid	6
Lunar	ar Partial Penumbral	
	Total Penumbral	11
	Partial Umbral	5
	Total Umbral	6

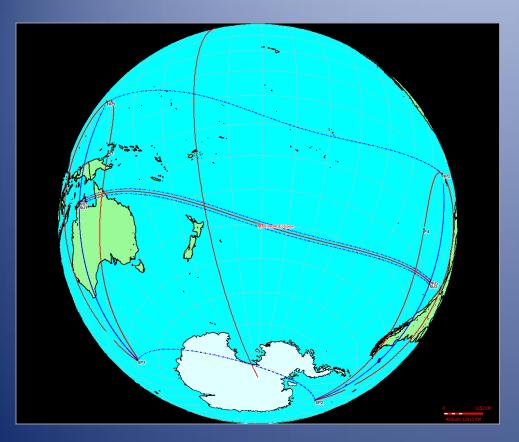
#### 2039 December 15th

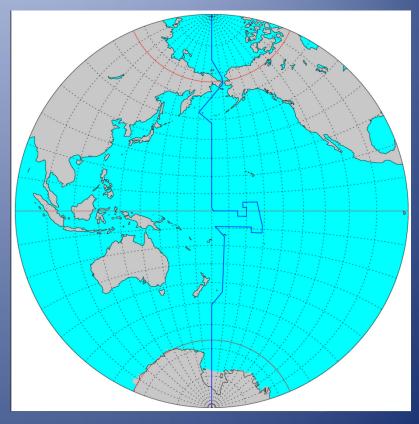


# Next eclipse to cross the International Date Line twice!



#### International date-line and eclipses





Australia 2012 – classic case

Crossed the date-line once

Go west = add one day

Go east = subtract one day

Kiribati adjustment January 1<sup>st</sup> 1995 Theoretically possible to cross date-line several times! Rob van Gent pages on web



#### Panorama Patterns

- Visualising the saros series
- Graphical explanation
  - Semester
  - The hidden relationship
- Tying up the loose ends

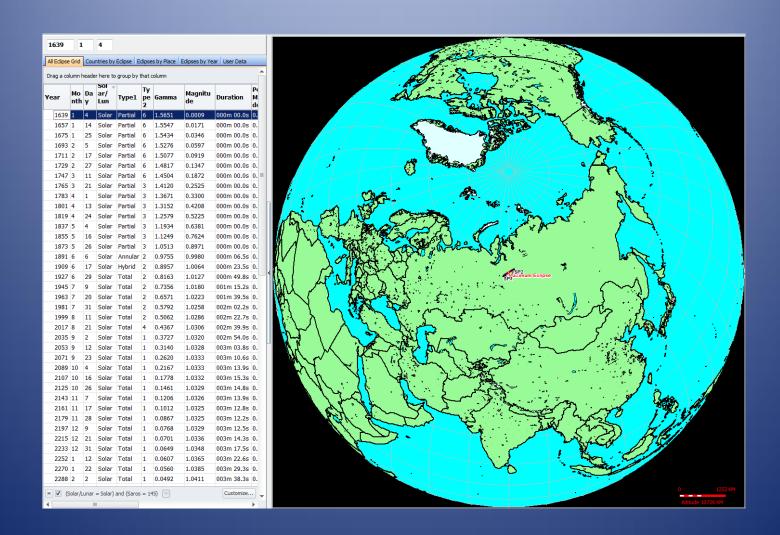
#### Saros

#### • 223 lunations

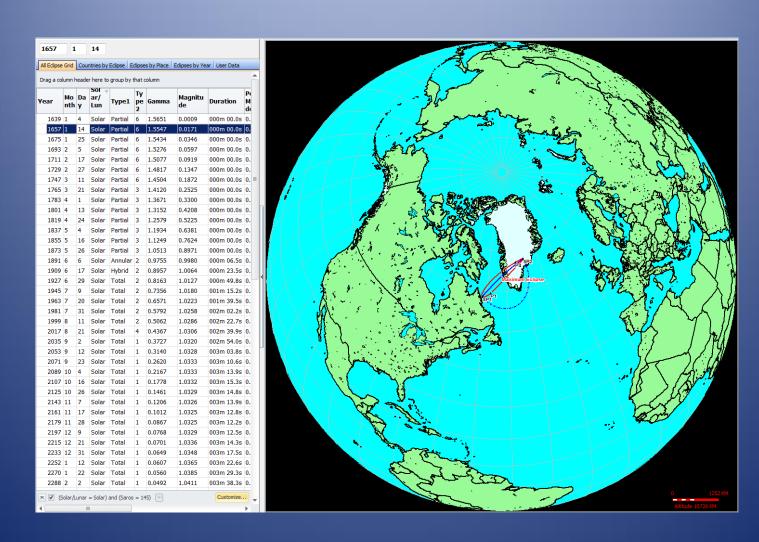
Moon's orbital cycle	Length in days	Number of periods	Days
Synodic month - (new moon to new moon)	29.530589	223	6585.3223
Anomalistic month – (perigee to perigee)	27.554550	239	6585.5375
Draconic month - (node to node)	27.212221	242	6585.3575

approximately 18 years 11 days 8 hours

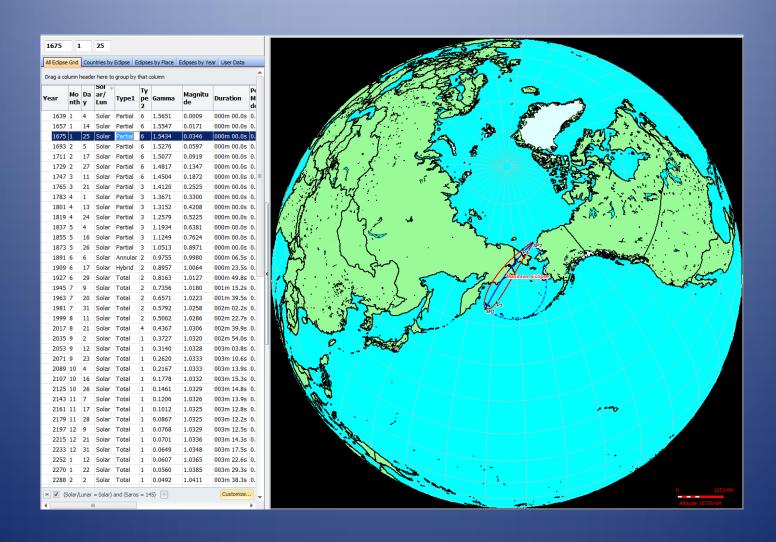
#### Saros 145 start 1639 partial

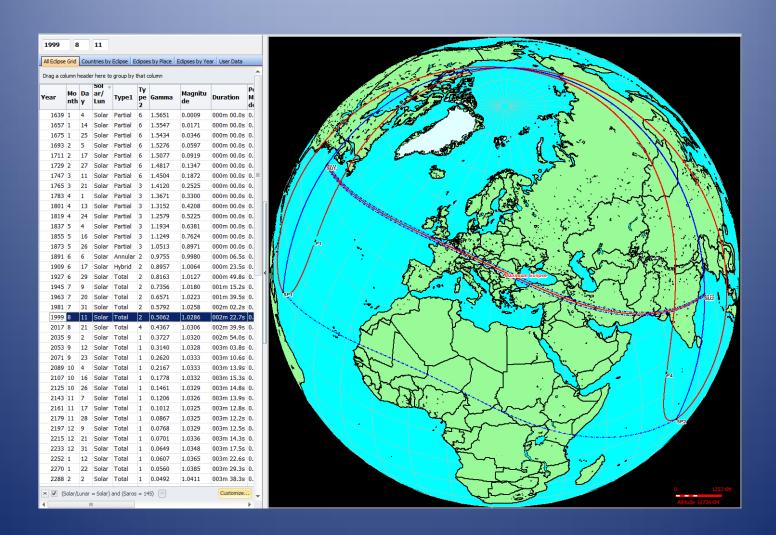


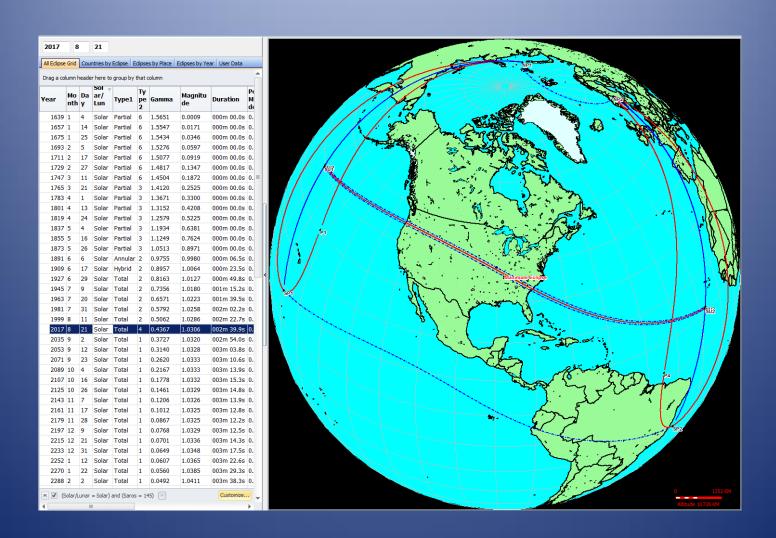
#### 1657 partial

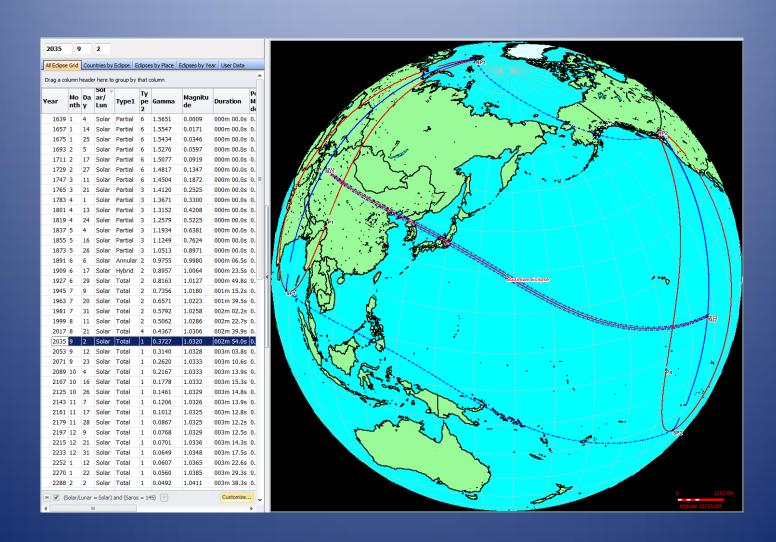


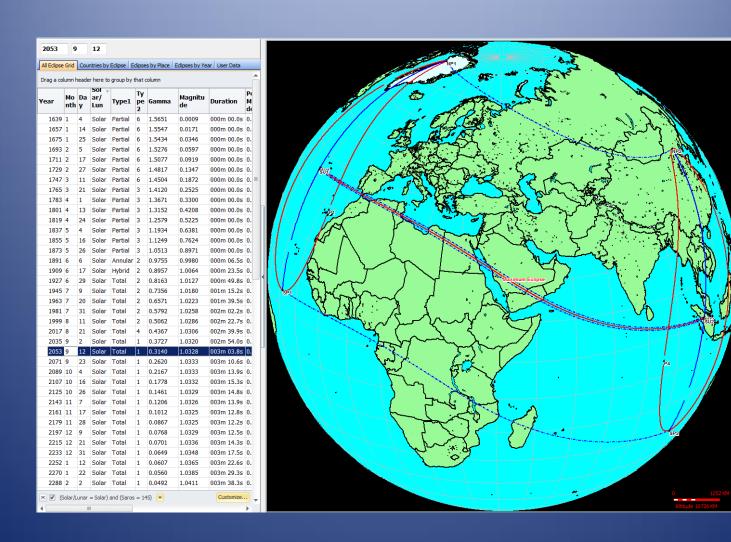
#### 1675 partial

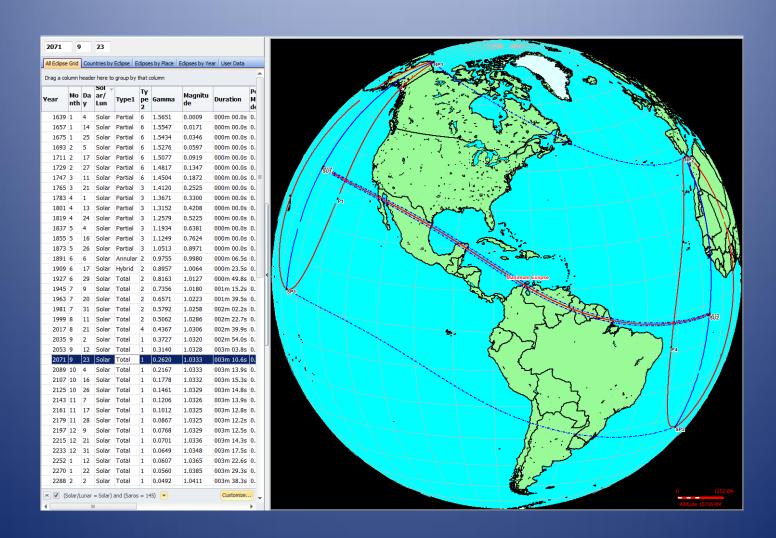




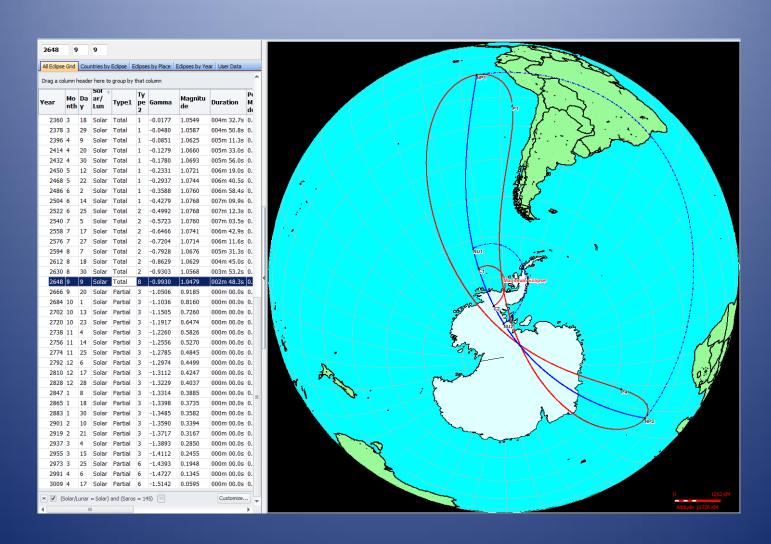




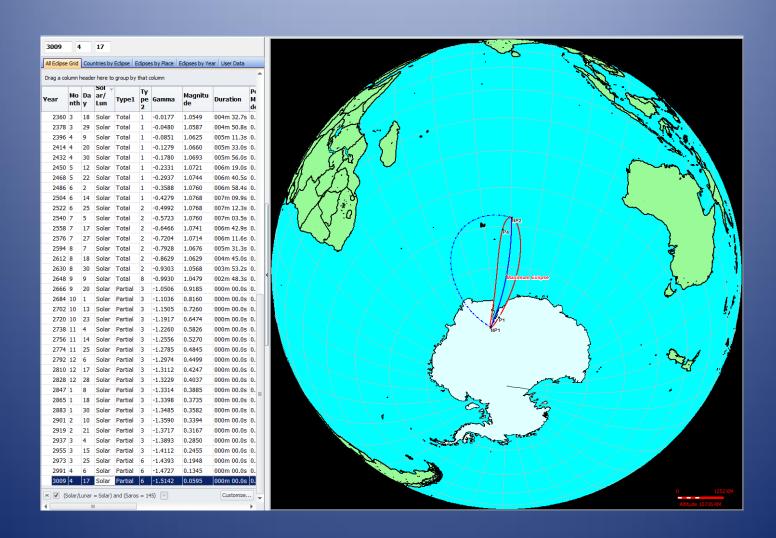




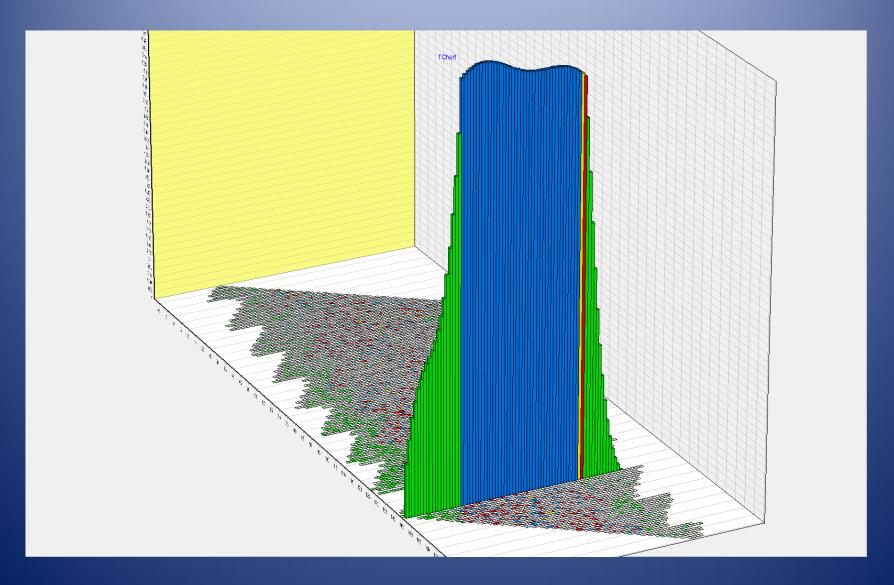
#### 2648 last total



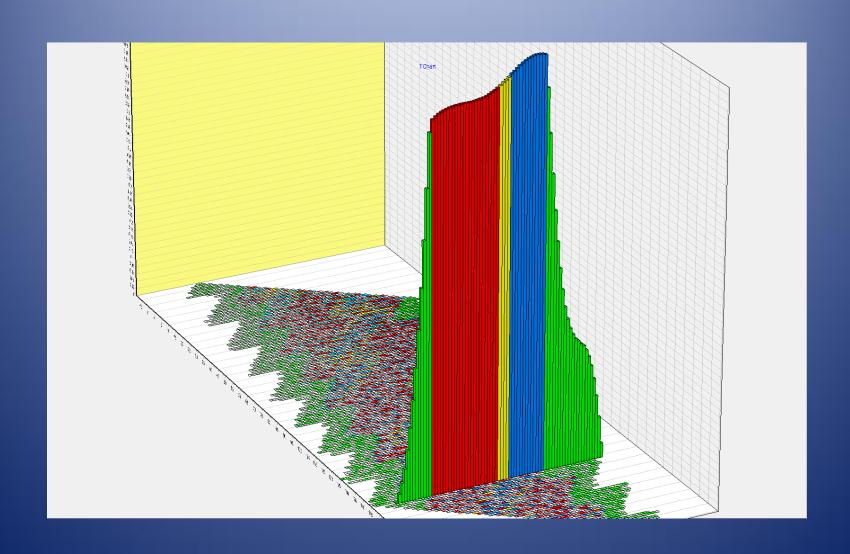
#### 3009 last partial



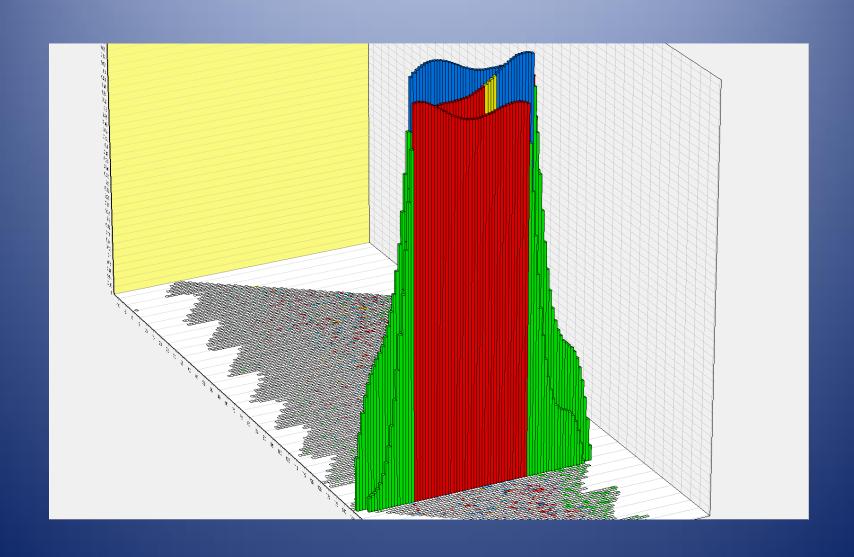
### Saros 145



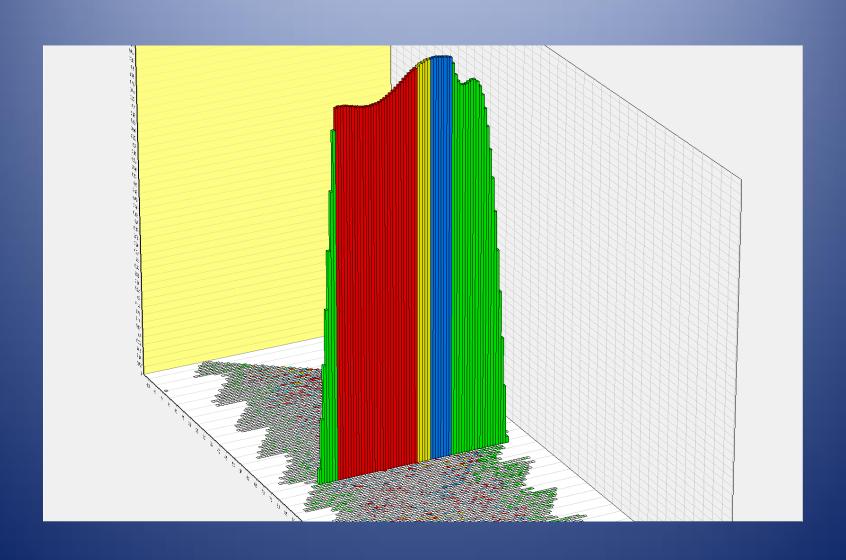
#### Saros 146



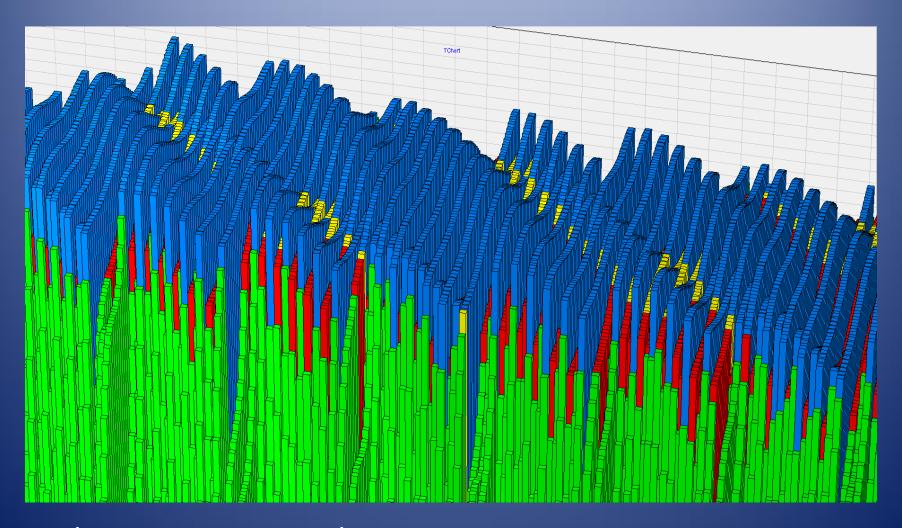
#### Saros 145, 146 and 147



#### Saros 76 – 3 maxima



#### Stack the solar saros side-by-side



Each saros series is 358 lunations apart = 1 inex

#### The Inex

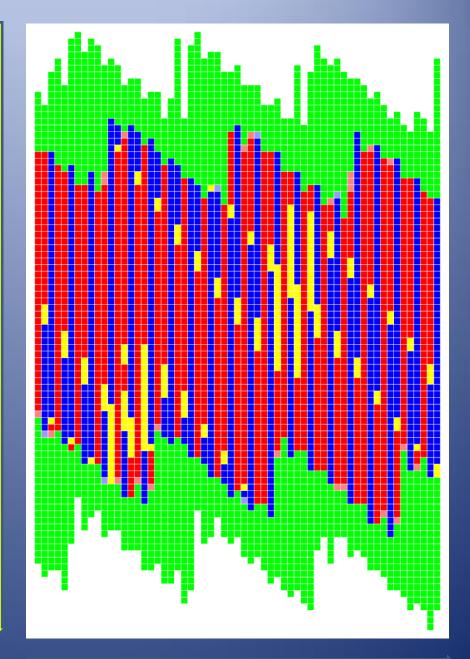
- 358 lunations
- Stack the saros series one inex apart

Moon's orbital cycle	Length in days	Number of periods	Days
Synodic month	29.530589	358 lunations	10571.9509
Anomalistic month	27.554550	383.67	10571.8542
Draconic month	27.212221	388.5	10571.9479

358 lunations - approximately 29years 11days

#### Solar Saros-Inex Panorama

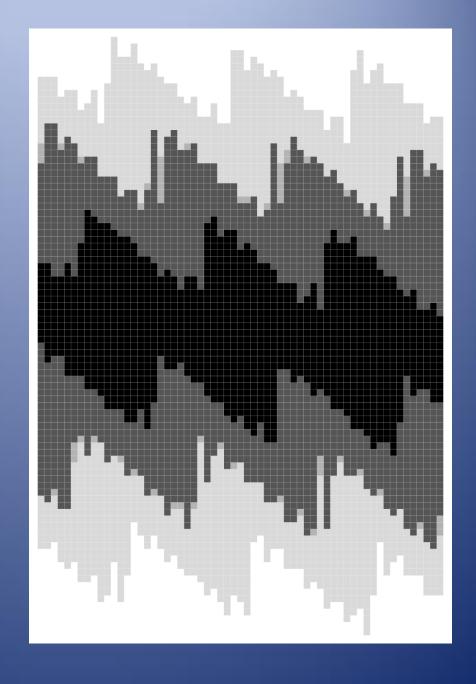
Saros 90 to 150



Saros

#### Lunar Saros-Inex Panorama

- •Saros 90 to 150
- In increasing order of shading
  - Partial penumbral
  - Total penumbral
  - Partial umbral
  - Total umbral

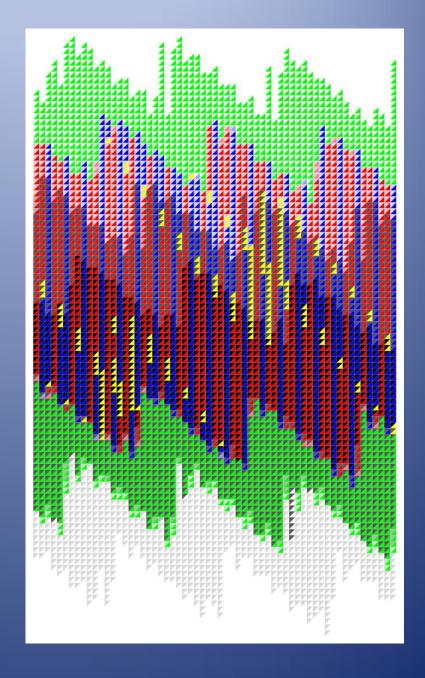


#### Can we combine the two panorama?

- Crazy idea!
- Why not?

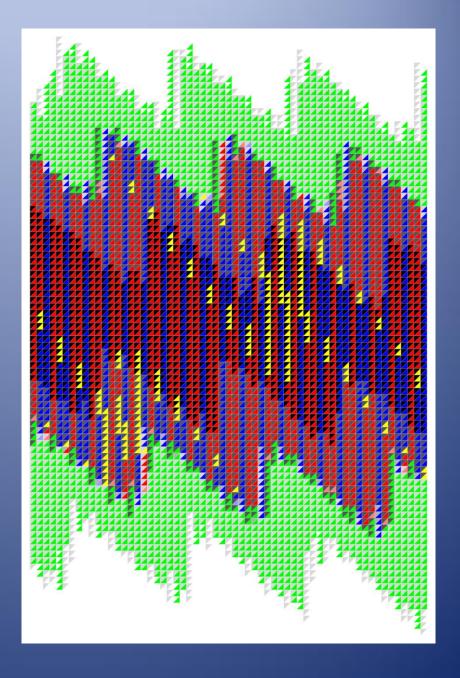
#### A merged Panorama

- First attempt
- Using corresponding saros and inex numbers
- Poor overlap

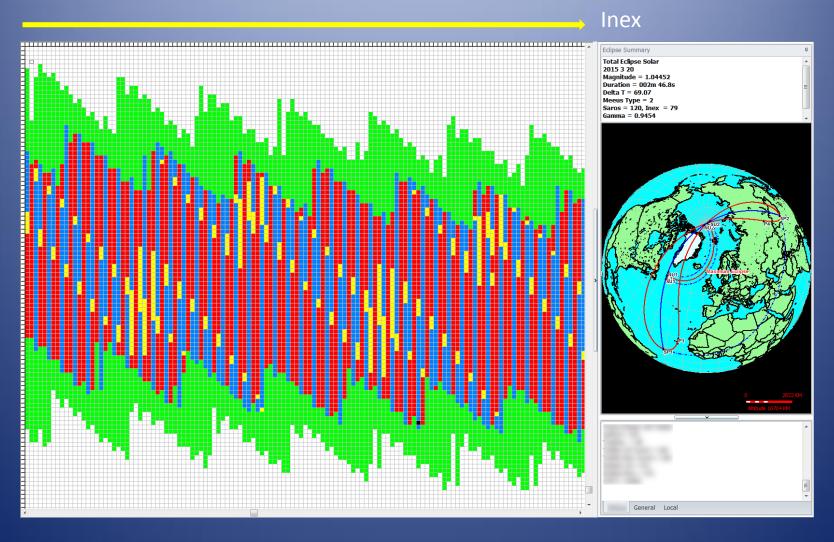


## The merged Panorama

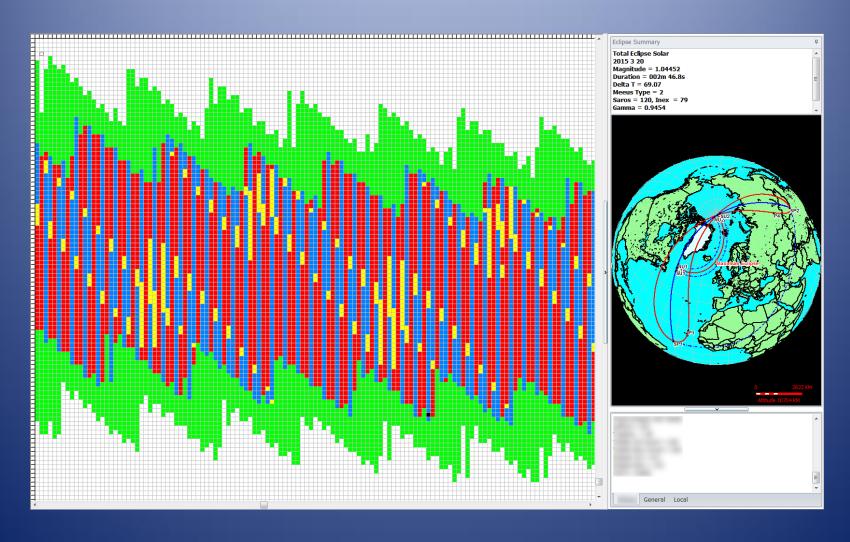
- Renumber the lunar saros and inex
- Luca Quaglia's idea
- LQ Saros = Saros + 7
- LQInex = Inex + 12
- Result is half a saros offset



#### The Solar Saros-Inex Panorama

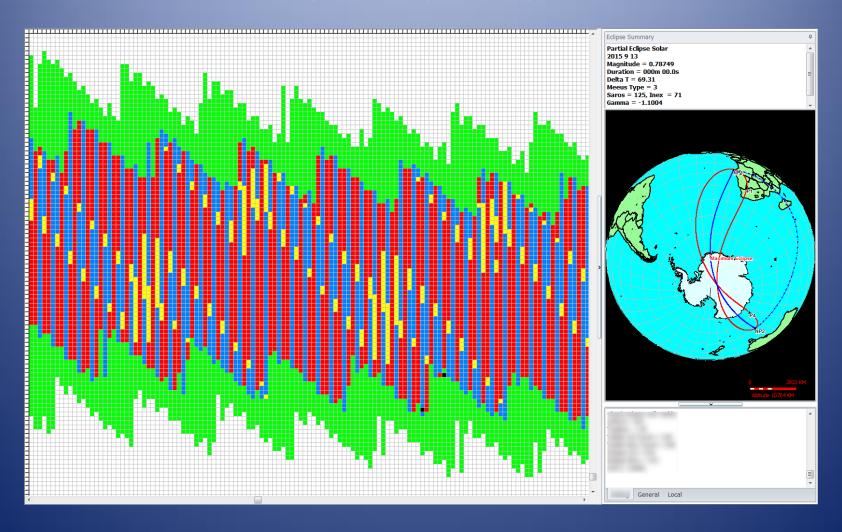


#### Solar Semester starts 2015 March 20<sup>th</sup>



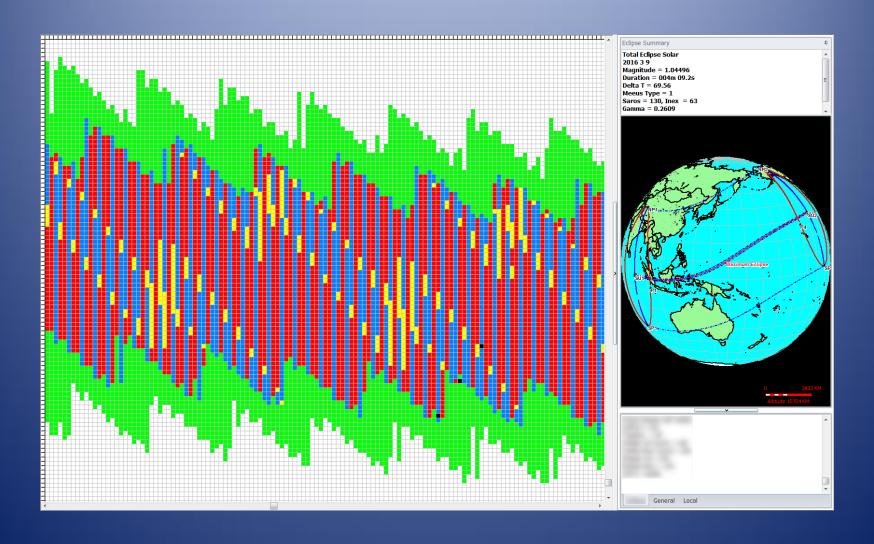
#### 2015 Sept 13<sup>th</sup>

#### 6 lunations later



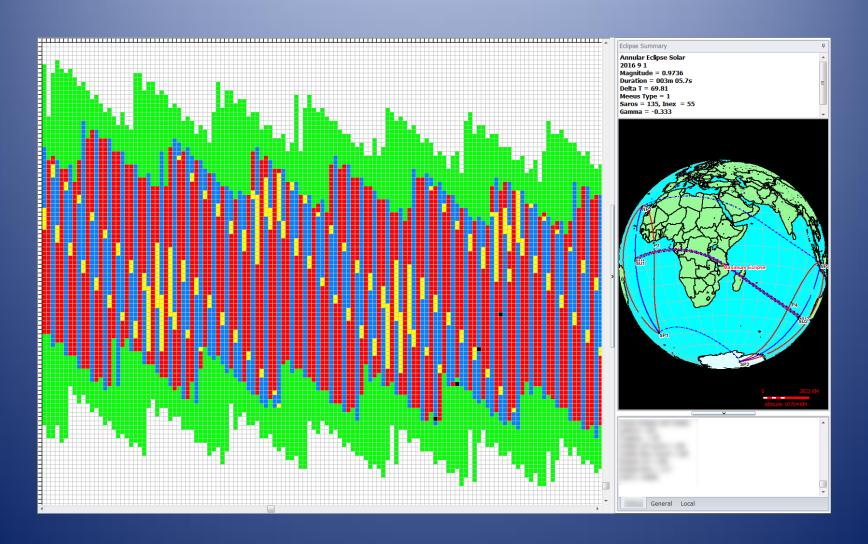
6 lunations = 5inex – 8saros or (5\*358 - 8\*223) = 6 lunations

#### 2016 March 9<sup>th</sup> 6 lunations later

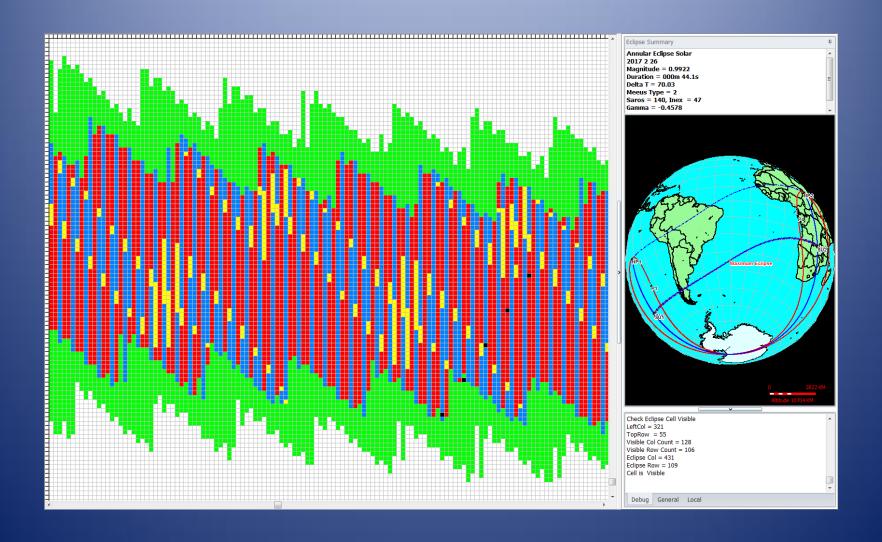


#### 2016 Sept 1st

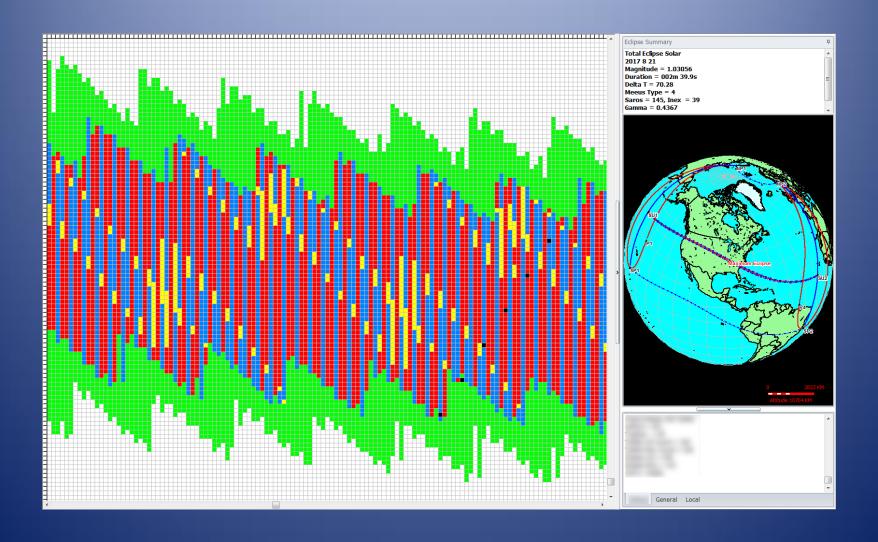
6 lunations later



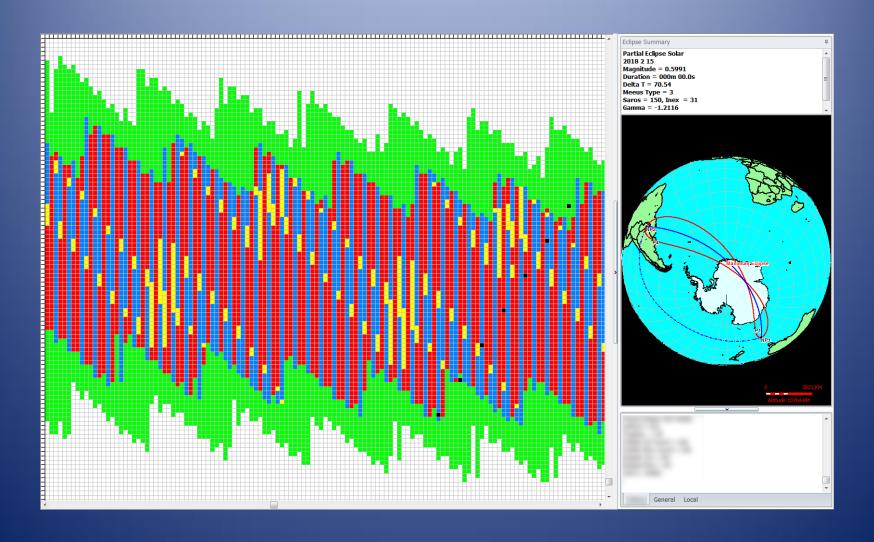
# 2017 Feb 26<sup>th</sup> 6 lunations later



#### 2017 Aug 21<sup>st</sup> 6 lunations later

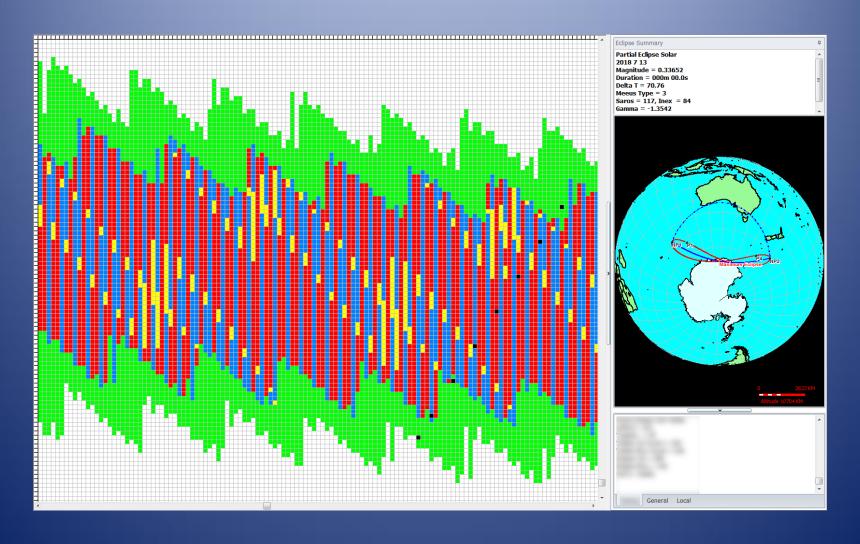


# 2018 Feb 15<sup>th</sup> 6 lunations later



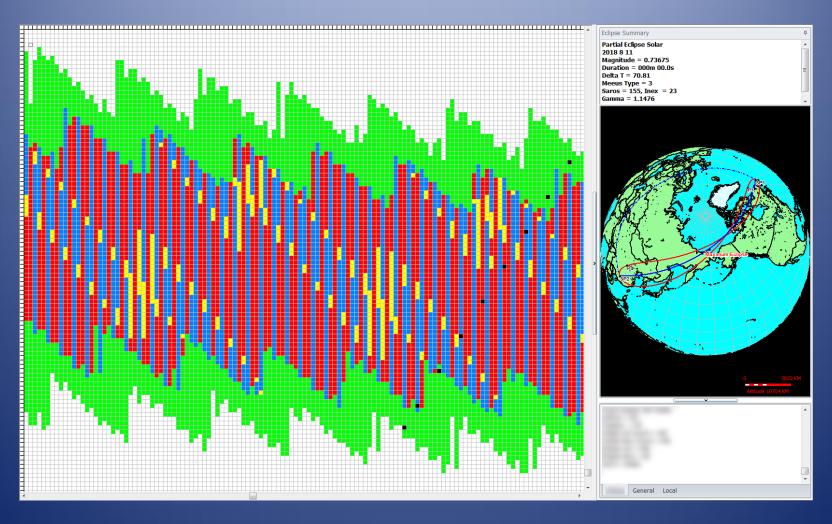
#### 2018 July 13<sup>th</sup>

5 lunations later = big jump back down

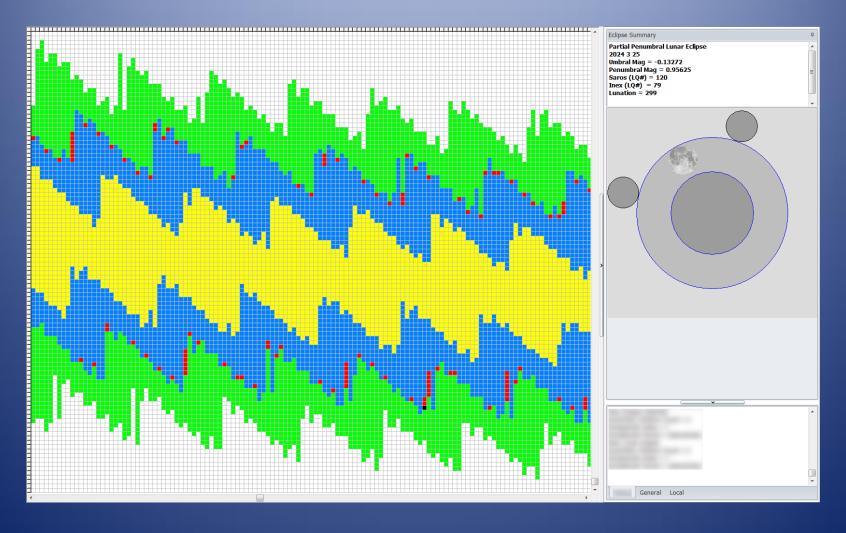


## 2018 Aug 11<sup>th</sup> 1 lunation later so really big jump back up

5+1 = 6 lunations after last but one eclipse

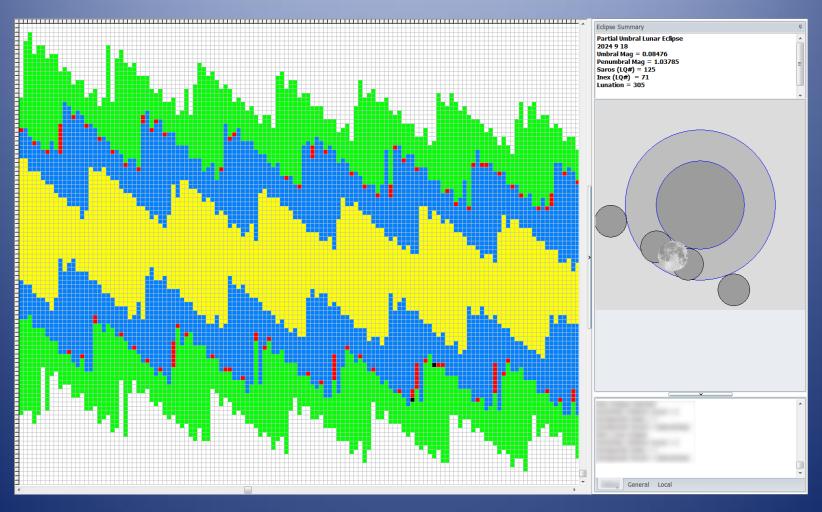


#### Lunar Semester – start half a saros later = 2024 March 25th



### 2024 Sept 18<sup>th</sup>

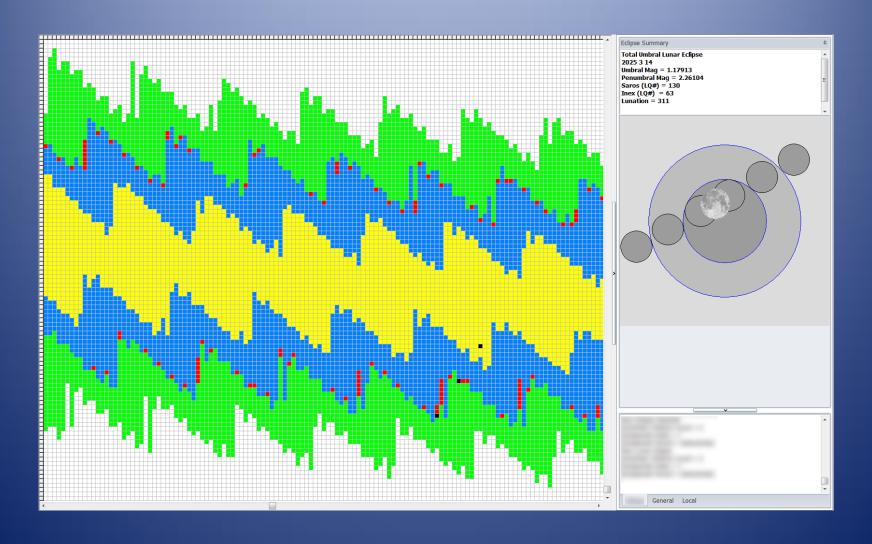
6 lunations later



6 lunations = 5inex - 8saros or (5\*358 - 8\*223) = 6 lunations

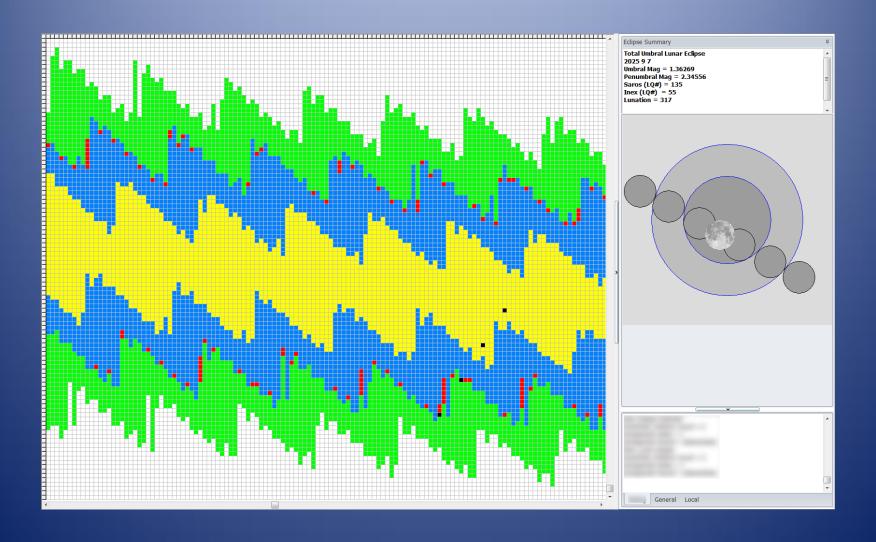
## 2025 March 14<sup>th</sup>

6 lunations later



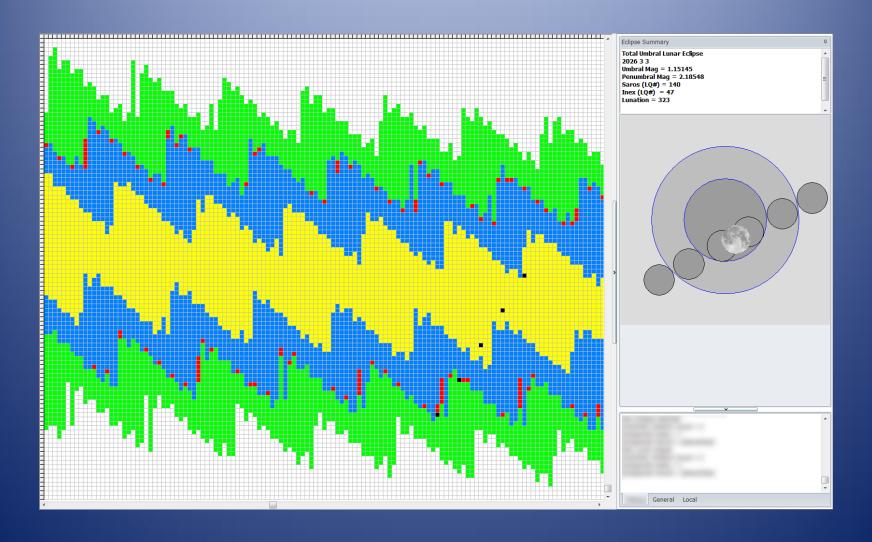
## 2025 Sept 7<sup>th</sup>

6 lunations later



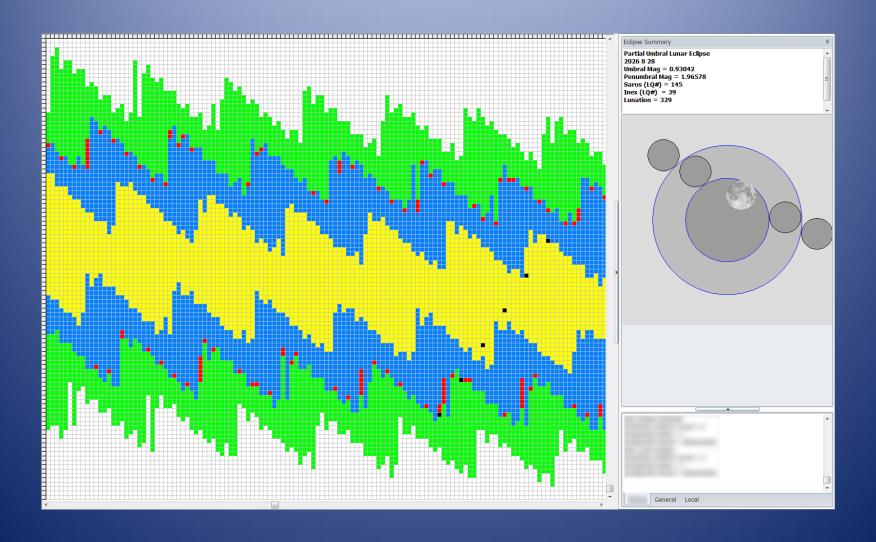
#### 2026 March 3rd

6 lunations later



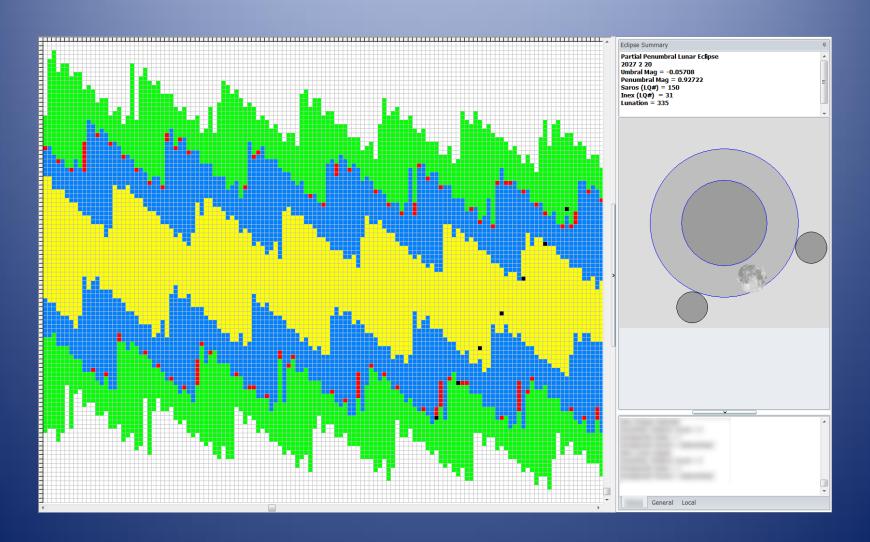
# 2026 Aug 28<sup>th</sup>

6 lunations later



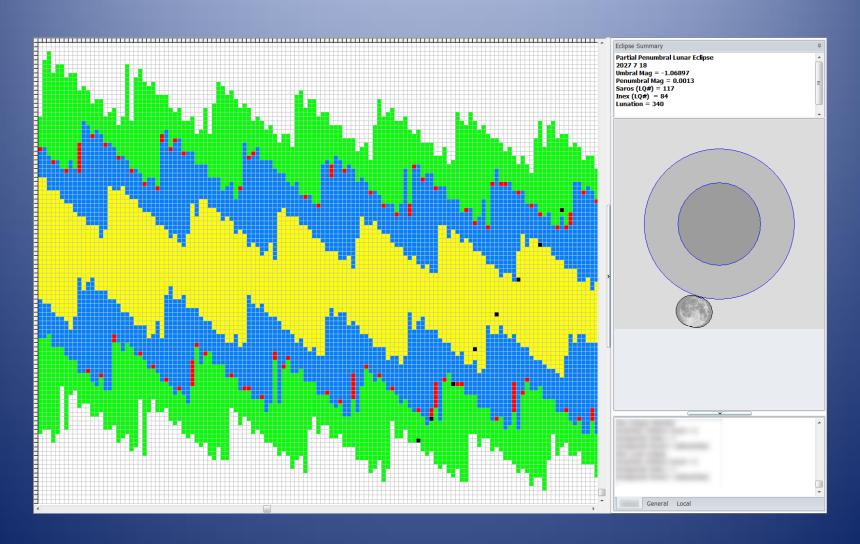
#### 2027 Feb 20<sup>th</sup>

6 lunations later



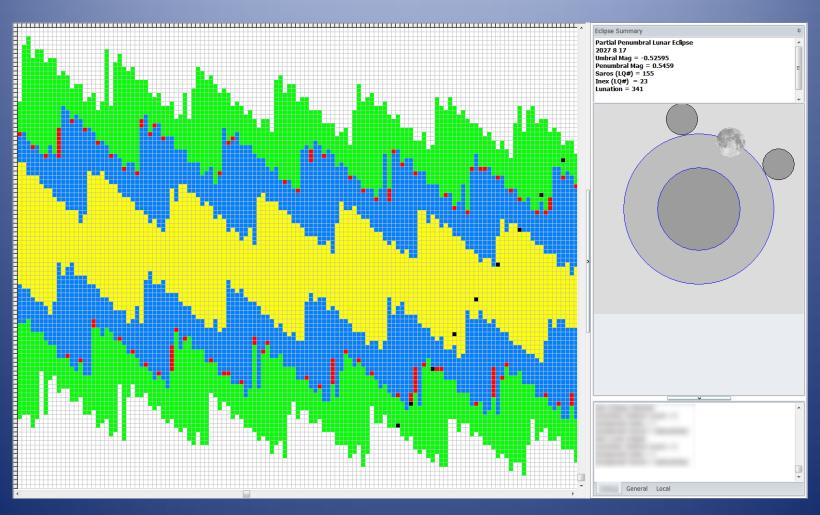
### 2027 July 18<sup>th</sup>

5 lunations later = big jump back down

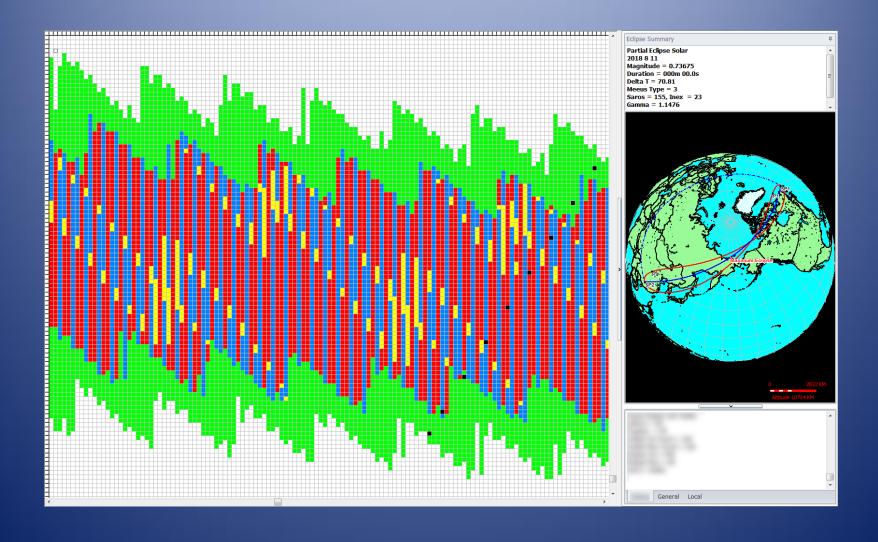


# 2027 Aug 17<sup>th</sup> 1 lunation later so really big jump back up

5+1 = 6 lunations after last but one eclipse

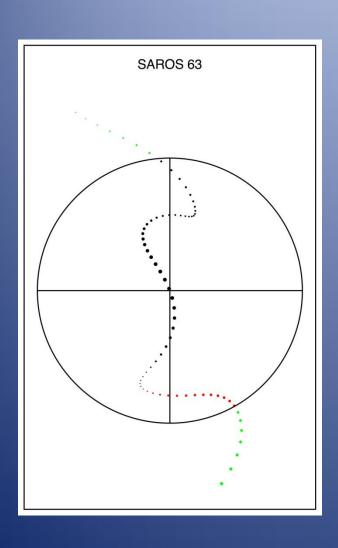


#### The solar-lunar semester fit



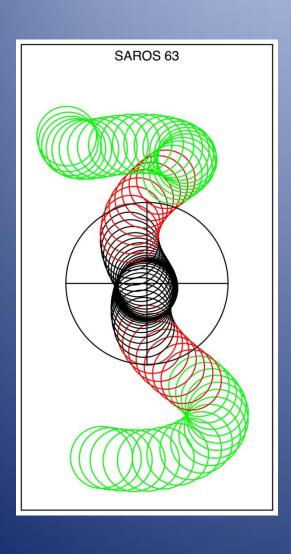


#### Leingartner Diagrams - 1

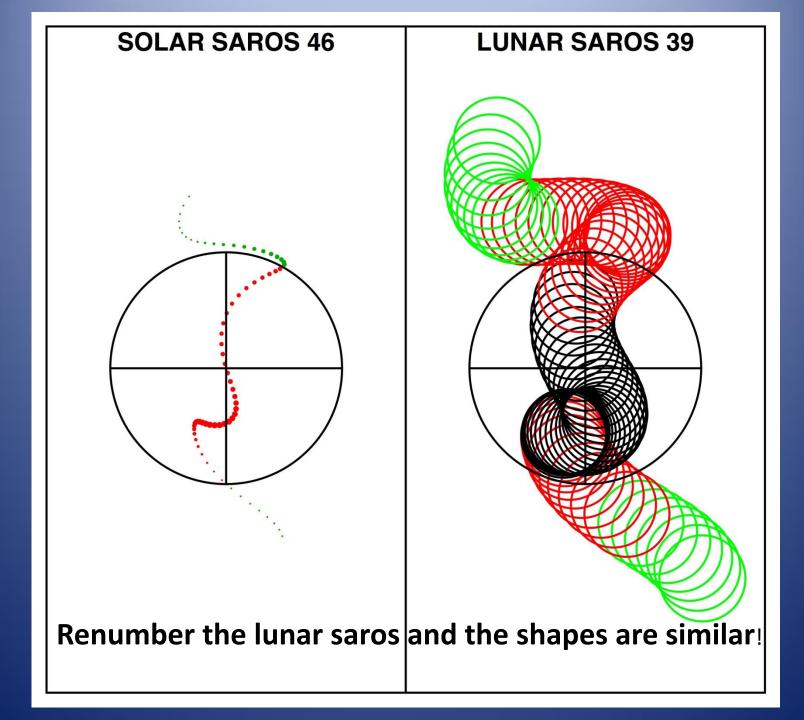


- Morsels 5
- "Saros Portraits"
- All eclipses in a saros
- Solar eclipses Earth and (ant)umbra shadow for each eclipse at maximum

#### Leingartner Diagrams - 2

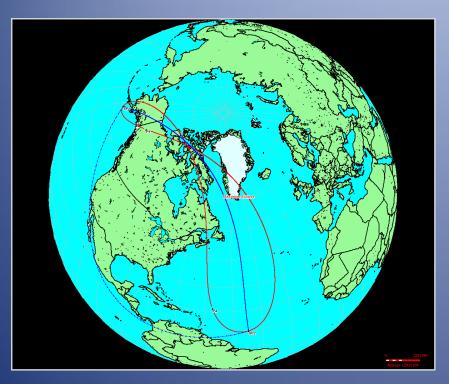


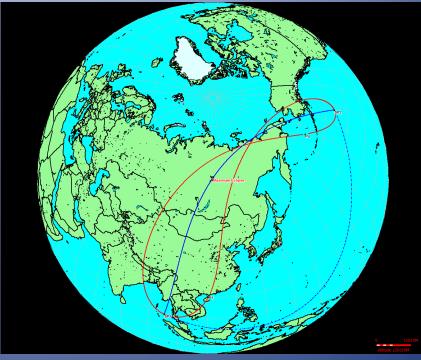
- "Lunar Worms"
- Umbral shadow fixed size
- Change size of the moon



# Tying up the loose ends

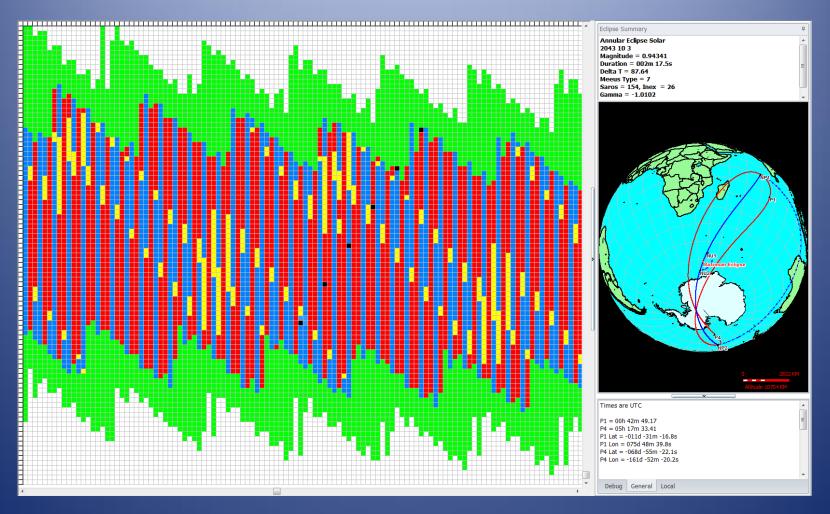
#### 2 Partial eclipses 77 lunations apart





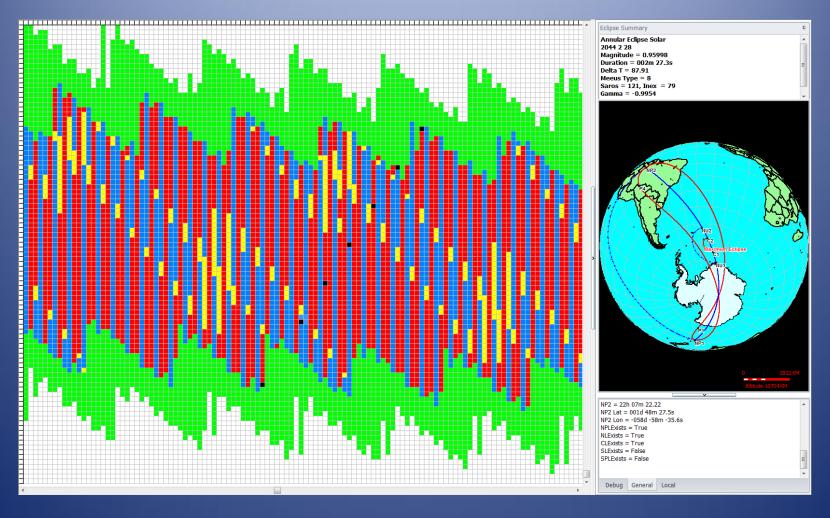
12 consecutive total or annular eclipses Visualised on the saros-inex panorama

#### 77 Iunation Gap



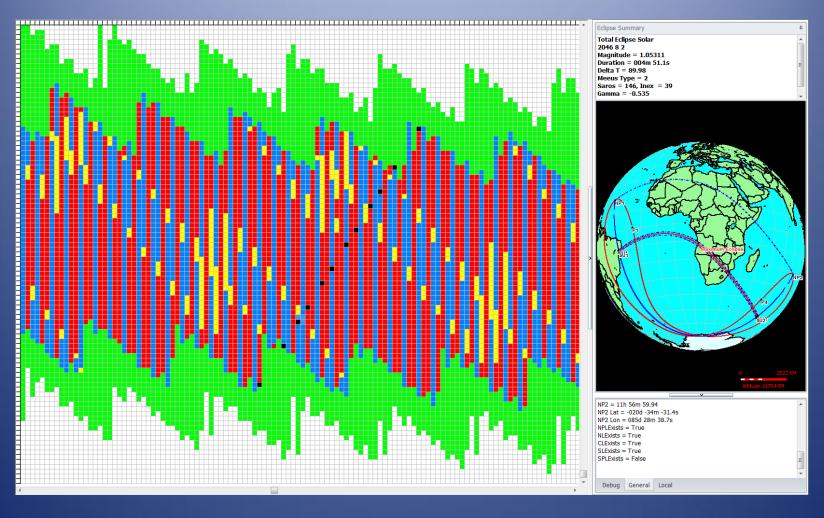
First 6 eclipses are 6 lunations apart – each annular or total

#### 77 Iunation Gap — (part 2)



Gap to 7<sup>th</sup> eclipse is 5 lunations – but this is an annular eclipse!

#### 77 Lunation gap – (part 3)



Next 5 eclipses are 6 lunations apart – each annular or total – so 12 consecutive annular or total eclipses!

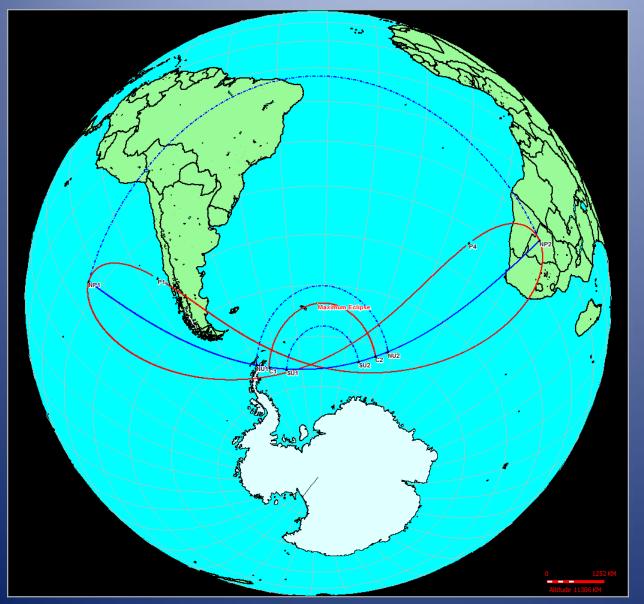


#### Quiz Question 3

 "Sines, Cosines and Tangents, apparently they were very important" ... "most helpful in" ... "foretelling eclipses, the arrival of comets and such like. I am very glad there are quite a number of people born with a gift and a liking for all of this" ... "I hope the Mathematicians" ... "are well rewarded. I promise never to blackleg their profession nor take the bread out of their mouths."



# Quiz 1 = Can you see totality in Antarctica at the summer solstice?



Yes, in theory
No in practice
Six days later

Total eclipse 1107 June 22<sup>nd</sup>

Solstice 1107 June 16th

#### Quiz 3 = Winston Churchill

 "Sines, Cosines and Tangents, apparently they were very important" ... "most helpful in" ... "foretelling eclipses, the arrival of comets and such like. I am very glad there are quite a number of people born with a gift and a liking for all of this" ... "I hope the Mathematicians" ... "are well rewarded. I promise never to blackleg their profession nor take the bread out of their mouths."



#### More Morsels Summary

- Eclipses by Country use digital data
  - Maximum eclipse MUST lie on the border
- 5 interesting eclipses
  - Gaps of 5 and 77 lunations
- Visualising the saros
- Panorama patterns for a graphical explanation
  - Semester
  - Renumber the lunar saros and inex
  - Lunation gaps on saros-inex panorama

#### Credits

- Luca Quaglia
  - 26000 year canon of solar and lunar eclipses
  - The half saros and renumbering the lunar saros and inex
  - Brain-storming eclipses by country
  - Drawing the Leingartner diagrams
  - Drawing the merged saros-inex panorama