## More Morsels - SEC2014



## Getting hooked on Morsels

## "Shadow Painting the Globe"






## Two Topics

## List ALL UK eclipses



## Two Topics

List ALL UK eclipses


- Solar and lunar semester
- The hidden relationship
- Lunation gaps

PERIODICITY AND VARIATION<br>OF

SOLAR (AND LUNAR) ECLIPSES

PROF. DR G. VAN DEN bERGH

How many countries?


Challenge
Produce lists of ALL

- Partial
- Annular
-Total eclipses
For ALL
countries
-From -1999
To +3000
How???


## Country and mapping data



| Vector Data | Number |  |
| :--- | :--- | :--- |
| Sovereign States | 197 | Greenland part of Denmark |
| Countries | 254 | France includes some territories |
| Map Units | 291 | Australia includes remote island |
| Map SubUnits | 351 | USA = 48 states + Hawaii + Alaska |
| States/Provinces | 3671 | In most cases too much data |

## 254 Countries



France = Mainland France, Corsica, French Guyana, Caribbean, Indian Ocean.

## 291 Map Units



France = Mainland France and Corsica

## Romania



5 layers of data = Country border, lakes, rivers, roads and built-up areas Country border is key

## Romania border as points



1201 pairs of border points in NEV10m - there are some "large" gaps Can find local circumstances for EACH border point Eclipse $\mathrm{Y} / \mathrm{N}$, type, magnitude - hence max eclipse on country border

## Country maximum eclipse MUST lie on the border



## Luca's Algorithm

"For any given country and for any given solar eclipse, the point of country maximum eclipse must lie on that country's border, unless the point of maximum for the eclipse as a whole lies inside that country. "


Track of totality crosses
Romania
-Romania sees a total eclipse

- Point of maximum for the eclipse as a whole (August 1999) actually lies inside Romania

Track of totality lies outside Romania
-Romania sees a partial eclipse -Max eclipse visible in Romania must lie on the border

Track of totality crosses Romania

- Romania sees a total eclipse
Max eclipse visible in Romania must lie on the border


## Eclipses by Country Number Crunching

- Natural Earth Vector 1:10million
- 291 "countries"
- 553176 points
- 11898 solar eclipses
- 6.58 billion calculations
- Note - some special cases
- Not yet fully handled



## USA Solar Eclipses



617 total
723 annular 3810 partial

In 5000 years

- 8 total eclipses exceed 6minutes duration in USA
- 2045 August $12^{\text {th }}$ total 6 m 6sec
- 12 lunations after 2044 Aug $23^{\text {rd }}$ total eclipse


## Eclipses with most countries to see totality or annularity



1433 June $17^{\text {th }}$
Total in 39 countries

-1763 October $8^{\text {th }}$
Annular in 53 countries

## Eclipses visible in most countries



Total eclipse 1600 July $10^{\text {th }}$ 212 countries Total in 11 countries Partial in 201 countries


Annular eclipse 410 June $18^{\text {th }}$ 210 countries
Annular in 11 countries Partial in 199 countries

## Total Eclipses by Country

- 3171 pure total
- 571 hybrid eclipses in 5000 years

|  | A |  | D |  |
| :---: | :--- | :--- | :--- | :---: |
| 1 | Country |  | \#Total |  |
| 2 | Russia |  | 634 |  |
| 3 | United States of America |  | 617 |  |
| 4 | Brazil | 495 |  |  |
| 5 | China | 459 |  |  |
| 6 | Canada | 447 |  |  |
| 7 | Australia | 427 |  |  |
| 8 | Antarctica | 392 |  |  |
| 9 | India |  | 355 |  |
| 10 | Chile | 347 |  |  |
| 11 | Indonesia | 321 |  |  |
| 12 | Argentina | 302 |  |  |
| 13 | Japan | 256 |  |  |
| 14 | Democratic Republic of the Congo | 245 |  |  |
| 15 | Mexico |  | 241 |  |
| 16 | Kazakhstan |  | 213 |  |
| 17 | Algeria |  | 213 |  |
| 18 | Colombia |  | 213 |  |
| 19 | Sudan |  | 207 |  |
| 20 | Peru |  | 196 |  |
| 21 | Saudi Arabia |  |  |  |
|  |  |  |  |  |

## Annular Eclipses by Country <br> -3956 pure annular <br> - 571 hybrid in 5000

 years| , | A | B | D |
| :---: | :---: | :---: | :---: |
| 1 | Country | \#Annular | \#Total |
| 2 | United States of America | 723 | 617 |
| 3 | Russia | 698 | 634 |
| 4 | Antarctica | 567 | 392 |
| 5 | Brazil | 546 | 495 |
| 6 | Australia | 510 | 427 |
| 7 | Canada | 490 | 447 |
| 8 | China | 489 | 459 |
| 9 | Chile | 412 | 347 |
| 10 | India | 402 | 355 |
| 11 | Indonesia | 376 | 321 |
| 12 | Argentina | 370 | 302 |
| 13 | Japan | 288 | 256 |
| 14 | Democratic Republic of the Congo | 273 | 245 |
| 15 | Mexico | 272 | 241 |
| 16 | Peru | 255 | 196 |
| 17 | Kazakhstan | 244 | 213 |
| 18 | Algeria | 242 | 213 |
| 19 | French Polynesia | 233 | 157 |
| 20 | Myanmar | 231 | 190 |
| 21 | Mozambique | 231 | 167 |

## Special Case 1

- Eclipse track is very narrow and passes between adjacent points on boundary
- Eclipse misclassified
- Hybrid eclipse 164 March $10^{\text {th }}$ in Peru
- Totality 3 seconds
- Use binary search to find point of greatest eclipse on boundary


## Special Case 2

- 2379 March $19^{\text {th }}$
- Grazes Austrian border
- Amount of detail in digital mapping can change the type or duration



## Special Case 3



- Lesotho is wholly inside South Africa
- Check "Point in country" algorithm implementation
returns correct country name!


## Aqueous Eclipses (MAM5)



Total eclipse 2310 May $29^{\text {th }}$ ( 5 m 10sec) misses all Pacific islands

## Aqueous total eclipses



Longest 6m 6s in 222 July


Next eclipse 2m 28s in 2057 Jan 5th

## 74 total aqueous eclipses in 5000 years

## Aqueous annular eclipses



Longest 10 m 44 s in -249 November


Next eclipse 22s in 2032 May 9th

## 97 annular aqueous eclipses in 5000 years

## Lunation Gaps

- Gaps between USA total eclipses
- Longest gap is 587 lunations
- Shortest gap is 6 lunations
- Gap to 2017 from 1991 is 323 lunations



## Quiz Question 1

- Can you see totality in Antarctica on the Summer Solstice - i.e. June?


## 5 interesting eclipses in next 35 years



## 2 Annular eclipses 5 lunations apart



Smallest possible gap between annulars
4 such pairs in 5 millenia Canon
Pair in -1461 overlap on land

## 2 Partial eclipses 77 lunations apart



77 lunations is longest gap in 5 millenia Canon and longest gap in 26000 year Canon 12 consecutive total or annular eclipses
Mentioned in Meeus "Elements of Solar Eclipses"

## Shortest gaps between eclipses

| Solar | Eclipse Type | Lunations |
| :--- | :--- | :--- |
|  | Partial | 1 |
|  | Pure Annular | $\mathbf{5}$ |
|  | Pure Total | 11 |
|  | Annular and hybrid | $\mathbf{5}$ |
|  | Total and hybrid | 6 |
| Lunar | Hybrid | 6 |
|  | Partial Penumbral | 1 |
|  | Total Penumbral | 11 |
|  | Partial Umbral | 5 |
|  | Total Umbral | 6 |

## 2039 December 15th



Next eclipse to cross the International Date Line twice!


## International date-line and eclipses



Australia 2012 - classic case
Crossed the date-line once
Go west = add one day
Go east = subtract one day


Kiribati adjustment January $1^{\text {st }} 1995$ Theoretically possible to cross date-line several times!
Rob van Gent pages on web


## Panorama Patterns

- Visualising the saros series
- Graphical explanation
- Semester
- The hidden relationship
- Tying up the loose ends


## Saros

## - 223 lunations

| Moon's orbital cycle | Length in days | Number of periods | Days |
| :--- | :--- | :--- | :--- |
| Synodic month <br> - (new moon to new moon) | 29.530589 | 223 | 6585.3223 |
| Anomalistic month <br> - (perigee to perigee) | 27.554550 | 239 | 6585.5375 |
| Draconic month <br> -(node to node) | 27.212221 | 242 | 6585.3575 |

approximately 18 years 11days 8 hours

## Saros 145 start 1639 partial



## 1657 partial



## 1675 partial



## 1999 total



## 2017 total



## 2035 total



## 2053 total



## 2071 total



## 2648 last total



## 3009 last partial



## Saros 145



## Saros 146



## Saros 145, 146 and 147



## Saros 76-3 maxima



## Stack the solar saros side-by-side



Each saros series is 358 lunations apart = 1 inex

## The Inex

- 358 lunations
- Stack the saros series one inex apart

| Moon's orbital cycle | Length in days | Number of periods | Days |
| :--- | :--- | :--- | :--- |
| Synodic month | 29.530589 | 358 lunations | 10571.9509 |
| Anomalistic month | 27.554550 | 383.67 | 10571.8542 |
| Draconic month | 27.212221 | 388.5 | 10571.9479 |

358 lunations - approximately 29years 11days

## Solar Saros-Inex Panorama

Saros 90 to 150

Saros


## Lunar Saros-Inex Panorama

- Saros 90 to 150
- In increasing order of shading
- Partial penumbral
- Total penumbral
- Partial umbral
- Total umbral



## Can we combine the two panorama?

- Crazy idea!
- Why not?


## A merged Panorama

- First attempt
- Using corresponding saros and inex numbers
- Poor overlap



## The merged Panorama

- Renumber the lunar saros and inex
- Luca Quaglia's idea
- LQ Saros = Saros + 7
- LQInex = Inex + 12
- Result is half a saros offset



## The Solar Saros-Inex Panorama



## Solar Semester starts 2015 March $20^{\text {th }}$



## 2015 Sept $13^{\text {th }}$

## 6 lunations later



6 lunations $=5$ inex -8 saros or $\left(5^{*} 358-8^{* 223}\right)=6$ lunations

## 2016 March 9th

## 6 lunations later



## 2016 Sept $1^{\text {st }}$

## 6 lunations later



## 2017 Feb 26th 6 lunations later



## 2017 Aug 21st 6 lunations later



## 2018 Feb 15 th 6 lunations later



## 2018 July $13^{\text {th }}$

## 5 lunations later = big jump back down



5 lunations $=53$ saros -33 inex or $(+53 * 223-33 * 358)=5$ lunations

## 2018 Aug 11 th

## 1 lunation later so really big jump back up

$5+1=6$ lunations after last but one eclipse


1 lunation $=38$ inex -61 saros or $(38 * 358-61 * 223)=1$ lunation

## Lunar Semester - start half a saros later $=2024$ March 25th



## 2024 Sept $18^{\text {th }}$ <br> 6 lunations later



6 lunations $=5$ inex -8 saros or $(5 * 358-8 * 223)=6$ lunations

## 2025 March $14^{\text {th }}$

## 6 lunations later



## 2025 Sept $7^{\text {th }}$ <br> 6 lunations later



## 2026 March $3^{\text {rd }}$

## 6 lunations later



## 2026 Aug 28 th <br> 6 lunations later



## 2027 Feb 20th <br> 6 lunations later



## 2027 July $18^{\text {th }}$

## 5 lunations later = big jump back down



## 2027 Aug 17 th

## 1 Iunation later so really big jump back up

## $5+1=6$ lunations after last but one eclipse



## The solar-lunar semester fit




## Leingartner Diagrams - 1



- Morsels 5
- "Saros Portraits"
- All eclipses in a saros
- Solar eclipses - Earth and (ant)umbra shadow for each eclipse at maximum


## Leingartner Diagrams - 2



- "Lunar Worms"
- Umbral shadow fixed size
- Change size of the moon


Tying up the loose ends

## 2 Partial eclipses 77 lunations apart



12 consecutive total or annular eclipses Visualised on the saros-inex panorama

## 77 lunation Gap



First 6 eclipses are 6 lunations apart - each annular or total

## 77 lunation Gap - (part 2)



Gap to $7^{\text {th }}$ eclipse is 5 lunations - but this is an annular eclipse!

## 77 Lunation gap - (part 3)



Next 5 eclipses are 6 lunations apart - each annular or total - so 12 consecutive annular or total eclipses!


## Quiz Question 3

- "Sines, Cosines and Tangents, apparently they were very important" ... "most helpful in" ... "foretelling eclipses, the arrival of comets and such like. I am very glad there are quite a number of people born with a gift and a liking for all of this" ... "I hope the Mathematicians" ... "are well rewarded. I promise never to blackleg their profession nor take the bread out of their mouths."



## Quiz 1 = Can you see totality in

## Antarctica at the summer solstice?



Yes, in theory No in practice
Six days later

Total eclipse
1107 June 22 ${ }^{\text {nd }}$

Solstice
1107 June 16th

## Quiz 3 = Winston Churchill

- "Sines, Cosines and Tangents, apparently they were very important" ... "most helpful in" ... "foretelling eclipses, the arrival of comets and such like. I am very glad there are quite a number of people born with a gift and a liking for all of this" ... "I hope the Mathematicians" ... "are well rewarded. I promise never to blackleg their profession nor take the bread out of their mouths."



## More Morsels Summary

- Eclipses by Country - use digital data
- Maximum eclipse MUST lie on the border
- 5 interesting eclipses
- Gaps of 5 and 77 lunations
- Visualising the saros
- Panorama patterns for a graphical explanation
- Semester
- Renumber the lunar saros and inex
- Lunation gaps on saros-inex panorama


## Credits

- Luca Quaglia
- 26000 year canon of solar and lunar eclipses
- The half saros and renumbering the lunar saros and inex
- Brain-storming eclipses by country
- Drawing the Leingartner diagrams
- Drawing the merged saros-inex panorama

